

Let  $G$  be a subset of the dual of a real Banach space  $X$  and  $F \subset G$ . Then  $F$  is a James boundary of  $G$  if each  $w^*$ -continuous linear functional on  $X$  attains its supremum over  $G$  on an element of the set  $F$ . We ask whether a norm bounded subset of  $X$  which is countably compact for the topology generated by  $F$  is necessary sequentially compact for the topology generated by  $G$ . The main content of our work is a positive solution to this problem. As a corollary we obtain James characterization of weakly compact subsets of a real Banach space. Due to the Eberlein-Šmuljan theorem a positive solution to the so called boundary problem is shown as a special case of the affirmative answer to the question raised above. The question is further discussed for a case of Banach spaces defined over the complex field. In this case we cannot use the old definition of the James boundary but by a “natural” way it is possible to redefine the term James boundary and then we are able to answer our question positively again.