In this thesis we deal with a numerical solution of time-dependent partial differential equations with the aid of numerical methods. Particularly, we focus on case, when different non-matching grids are employed on different time steps. Then piecewise polynomial approximate solution has to be recomputed from one mesh to the second one. We present the developed algorithm as well as several numerical tests.