

In the present work we study tetrahedral  $k$ -reptiles. A  $d$ -dimensional simplex is called a  $k$ -reptile if it can be tiled in  $k$  simplices with disjoint interiors that are all congruent and similar to  $S$ . For  $d = 2$ , triangular  $k$ -reptiles exist for many values of  $k$  and they have been completely characterized. On the other hand, the only simplicial  $k$ -reptiles that are known for  $d \geq 3$  have  $k = md$ , where  $m \geq 2$  (Hill simplices).

We prove that for  $d = 3$ , tetrahedral  $k$ -reptiles exist only for  $k = m^3$ . This partially confirms the Hertel's conjecture, asserting that the only tetrahedral  $k$ -reptiles are the Hill tetrahedra. We conjecture that  $k = md$  is necessary condition for existence of  $d$ -dimensional simplicial  $k$ -reptiles,  $d \geq 3$ .