The thesis presents different algebraic approaches to solving high school geometry problems. In particular, it shows the use of circle pencils, Desargues involution, the Method of Animation, and elliptic curves. It contains selected problems with solutions to show how these techniques can solve different problems.