# CHARLES UNIVERSITY FACULTY OF SOCIAL SCIENCES <br> Institute of Economic Studies 



# Analysis of the US Stock Market during the COVID-19 pandemic 

Bachelor's thesis

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## Declaration of Authorship

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#### Abstract

This work investigates the effect of the COVID-19 pandemic on the S\&P 500 stock index and its eleven sectors. Employing the ARMA and the T-GARCH model on a time series of daily returns from 2018 until March 2021, we examine the impact on volatility, returns, and day-of-the-week effect during the stock market crash caused by the pandemic and the period after. Our main findings imply that in the case of returns, the Monday effect was more negative than the Friday effect during the market crash and vice versa in the rising market after the crash. Concluding that the calendar time hypothesis holds for the observed periods. In terms of volatility, it drastically increased across the US stock market during and even after the crash. The increase was especially noticeable for the IT and Energy sectors. We also found the U-shaped daily volume pattern changed significantly with proportionately less volume of trades happening in the first half-hour of trading and more throughout the whole day. | JEL Classification | C22, C52, C58, G01, G14 |
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#### Abstract

Abstrakt

Tato práce zkoumá vliv pandemie COVID-19 na americký akciový index S\&P 500 a jeho jedenáct sektorů. Pomocí modelů ARMA a T-GARCH na časové řadě denních výnosů od roku 2018 do března 2021 zkoumáme dopad na volatilitu, výnosy a efekt dne v týdnu během krachu akciového trhu způsobeného pandemií a období po něm. Naše hlavní zjištění naznačují, že v případě výnosů byl pondělní efekt během propadu trhu víc negativní než páteční efekt a na rostoucím trhu po pádu naopak. Docházíme tedy k závěru, že pro sledovaná období platí hypotéza kalendářního času. Pokud jde o volatilitu, ta dramaticky vzrostla na celém americkém akciovém trhu jak během propadu, tak i po něm. Nárust zaznamenala zejména odvětví informačních technologií a energetiky. Zjistili jsme také, že se významně změnil denní objemový vzor obchodování ve tvaru písmene "U" s úměrně nižším objemem obchodů v první půlhodině obchodování a vyšsím během zbytku dne. | Klasifikace JEL | C22, C52, C58, G01, G14 <br> akciový trh, GARCH, objem obchodů, pan- <br> demie, volatilita |
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## Acronyms

ACF Autocorrelation Function
ADF Augmented Dickey-Fuller
ANOVA Analysis of variance
AR Autoregressive
ARCH Autoregressive Conditional Heteroscedasticity
ARMA Autoregressive Moving-Average
EMH Efficient Market Hypothesis
GARCH Generalized Autoregressive Conditional Heteroscedasticity
iid independent and identically distributed
MA Moving-Average
NYSE New York Stock Exchange
PACF Partial Autocorrelation Function
QE quantitative easing

# Bachelor's Thesis Proposal 

Author Adam Tůma<br>Supervisor prof. PhDr. Ladislav Krištoufek, Ph.D.<br>Proposed topic Analysis of the US Stock Market during the COVID-19 pandemic

Research question and motivation The main research question I intend to study is the effect the COVID-19 pandemic has had on the US stock market.

I would like to find out whether some new patterns can be observed on the stock market during a pandemic period, which are otherwise not present.

One of the possible patterns could be the well known day of the week effect that had been analysed many times before, in fact the first analysis was done in a journal article in the 1970s when it was shown that there is a tendency for the market to rise on Fridays and decline on Mondays (Cross, 1973). Over the years, many other analyses researching this phenomenon have been done, but I am especially interested in the possible patterns that may have arisen during the panic that was caused on the stock market due to the COVID-19 pandemic. I am keen to explore this, as my hypothesis is that the Monday effect was very strong in the first stages of the pandemic as more and more bad news were being published, however in my opinion this effect was rather short-lived as the initial panic on the market did not last very long.

During the last financial crisis in 2008, the stock market was hit especially hard in the financial sector with very high volatility (Schwert, 2011). However, that was largely due to the fact that the crisis started with the collapse of the housing markets, which was closely tied to the financial market, however, the COVID-19 crisis is very different. I am interested to test, whether some strong similarities can be seen in the behaviour of the stock market with what was researched for the Great Recession, or the market was hit much stronger in other fields. We can already see that companies in the technological sector are performing very well and I would like to explore the effects on various sectors and compare the results. I hypothesize that the market volatility was very high across all sectors in the early stages of the pandemic, and
then slowly forming some patterns. With the technological sector receiving a lot of attention during the crisis, I would assume higher volatility for this sector than usual.

My thesis will cover both the possible patterns in form of the day of the week effect as well as the patterns of volatility or trading volume across multiple sectors traded on the US stock market.

Methodology I will use publicly available sources (e.g. dukascopy.com, finance.yahoo.com etc.) where I can gather data points for the whole US stock market using the Standard Poor's index of 500 largest companies traded on the US stock market, as well as multiple other stocks representing the different fields that are being traded on the stock exchange (technology, financial sector, pharmaceuticals, energy...).

After gathering the data, I will analyze the day of the week effect, the volume being traded and the volatility during the given period. Then I will match the results from the COVID-19 period with results for past years and compare them with previous researches done and evaluate my hypotheses.

I would like to use statistical tests to measure the day-of-the-week effect as well as some more advanced econometric models like the GARCH model for estimating the market volatility.

Expected Contribution The topic of the COVID-19 pandemic and its effects on all types of markets is very fresh with still very little literature covering it. Which gives a great opportunity for this thesis to provide some interesting data, that have not yet been covered.

The main contribution this thesis will provide is the behaviour of the investors on the stock market during a crisis like this one. It will be very interesting to provide solid data on the different sectors of the economy and the impact the crisis has had on them.

## Outline

1. Introduction

- Motivation behind the topic
- Contribution
- Organization of the thesis

2. Literature review and hypotheses

- Literature on stock market analysis
- Evidence of existing patterns on the market
- Hypotheses

3. Data and methodology

- Description of the data
- Description of the methods used in the analysis
- Explaining how I perform the analysis

4. Results

- Interpreting the results
- Evaluating on hypotheses

5. Conclusion

- Broader interpretation and commenting on the results
- Implications for practice
- Topics for further research


## Core bibliography

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Author

## Chapter 1

## Introduction

On March 16, 2020, the New York Stock Exchange (NYSE) shut down all trading for 15 minutes for the third time within eight days. The trading halt is done automatically whenever the S\&P 500 index loses $7 \%$ compared to the previous day's closing price. The last time the circuit breaker was triggered before the pandemic crash was during the financial crisis in 2008. While the novel coronavirus was first discovered in Wuhan, China, at the end of 2019, and the first confirmed case in the USA was on January 21, 2020, there was no considerable attention regarding the situation visible on the US stock market as it still peaked on February 19, 2020. However, once the prices started to fall, the market quickly turned into a bear market ${ }^{1}$. The uncertainty of the evolving pandemic situation caused stock markets all around the world to crash, the S\&P 500 specifically plummeted more than $34 \%$ by March 23, 2020, to 2,237 index points, price levels last seen at the end of 2016. On March 23, 2020, $\mathrm{FED}^{2}$ announced extensive measures to support the American economy with unlimited quantitative easing (QE). In matter of weeks, FED's balance sheet increased from around 4 trillion USD before the pandemic to more than 7 trillion USD by June 2020. The announcement of unlimited QE proved to be the turning point at which the US stock market started regaining its losses and turned into a bull market once again. The S\&P 500 rebounded to a new alltime high on August 18, 2020, closing at 3,389 points. As of the thesis' writing, on April 16, 2021, the index closed at 4,185 points, up $86 \%$ from the lowest point over a year ago. And while it is obvious the pandemic was the cause of the stock market crash in 2020, the negative effect was relatively short-lived as

[^0]the pandemic still affects millions of people worldwide and has killed over half a million people in the USA alone. On the other hand, this opens opportunities for analysis of both periods, firstly the market crash between February and March of 2020, and secondly the period of high growth after that.

The objective of this thesis is to look for inefficiencies on the US stock market that may have arisen during the pandemic, thus observe some predictable patterns on the market. We will analyse the day-of-the-week effect, namely the Monday and Friday effect using conditional heteroscedastic models as the uncertainty of the evolving pandemic situation may have largely impacted investor's behaviour around weekends. We use data from S\&P 500 index and also data for eleven sectors of the S\&P 500 to measure the impact across sectors of the economy. As we mentioned, the pandemic caused the stock market to turn into a bear market only for about two months, which a strong bull market has followed ever since then. The effects in these two states of the market can differ significantly, which is why we will analyse the effects for the bear and bull market separately and get seperate results for the different time periods using dummy variables. We will also explore the intraday volume pattern, observing how the trading activity splits out during the day and how the pandemic affected it.

The thesis is further divided into the following chapters. Chapter 2 reviews the available literature relevant for our study and includes our hypotheses. Chapter 3 provides information about the data used and the outlined time periods for the purpose of this analysis. Chapter 4 describes the methodology used both for the conditional heteroscedastic models and the intraday volume analysis. Chapter 5 provides the empirical results of the analysis. And finally, Chapter 6 summarises our findings.

## Chapter 2

## Literature review and hypotheses

The amount of available literature on stock markets and the US stock market is explicitly vast, but it by no means implies that there is no room for new meaningful studies. Stock markets, in general, are very dynamic as they reflect many different variables on top of the traded companies' actual valuation, whether those variables are new trends among the traded companies, change in monetary policies, macroeconomic factors, current political situation, or perhaps most recently the COVID-19 pandemic.

This section will point out the relevant studies that have been done both historically and recently regarding market anomalies such as the day of the week effect or intraday volume patterns. We also cover recent literature related to COVID-19 effects on the stock market.

### 2.1 Market anomalies

The day of the week effect was initially studied by Osborne (1962), who studied various patterns on the US stock market. His results showed that the market tends to decrease on Mondays more likely than on other days. Many further studies in the 20th century were done studying the phenomenon of the day of the week effect (Cross 1973; French 1980; Gibbons \& Hess 1981; Jaffe \& Westerfield 1985; Jaffe et al. 1989; Lakonishok \& Maberly 1990). The studies' main conclusions include low average returns on Mondays, while Fridays tend to show higher returns than other days of the week.

Cross (1973) focused mainly on the Monday and Friday effect and concluded that the average returns on Mondays are significantly lower than on other days while also being heavily correlated to previous Friday returns. The correlation
was also shown by Jaffe et al. (1989) whose results showed that the Monday effect virtually disappears when the market has previously risen.

French (1980) developed two hypotheses for the Monday effect. Firstly, under the calendar time hypothesis, the average returns on Mondays should be three times higher than on other days as there are two non-trading days between Friday and Monday. And secondly, under the trading time hypothesis, the average returns on Mondays should be the same as for other days as returns are being generated only during trading time. His results showed that from 1953 to 1977, average Monday returns were significantly negative, while returns for other days of the week were positive. Thus both the trading and calendar time trading hypotheses were rejected. Kiymaz \& Berument (2003) used data from S\&P 500 between years 1972 and 1997, to measure the day of the week effect both in terms of return and volatility. Their findings show the lowest returns on Mondays and the highest returns on Wednesdays, which are also the most volatile based on their results.

Many studies are trying to find the possible explanations for the abnormally low Monday returns. Jain \& Joh (1988) found that the volume of S\&P 500 stocks traded on Monday is the lowest across all days and roughly $10 \%$ lower than the average of other trading days, with Wednesday volume being the highest. Lakonishok \& Maberly (1990) analysed the trading patterns of individual and institutional investors, and their results showed that individual investors tend to increase their activity on Mondays, concluding that the Monday effect might be due to the patterns in trading of individual investors.

While most of the famous studies covering the day of the week effect come from the previous century, there are still plentiful recent studies covering the topic. Zhang et al. (2017) employed the GARCH model on rolling samples of $500,1000,1500$ days to show the significance of the day of the week effect on multiple stock markets. For S\&P 500 index, they found that recently mainly Monday, Tuesday and Friday effect were statistically significant, especially ever since the end of the financial crisis of 2008-09, after which the US stock market has been in a very optimistic state also known as a bull market. Ülkü \& Rogers (2018) employed GJR-GARCH on data from Asian stock markets split by investor identification. Their finding showed that institutions' refraining from trading on Mondays emerges as a partial explanation of the Monday effect. It further supports earlier results of Lakonishok \& Maberly discussed in the previous paragraph.

Another anomaly relevant for our analysis is the intraday volume trading
pattern. Earlier studies show that the average trading volume across daily trading hours differs significantly on the US stock market. The highest activity occurs during the first trading hour and declines slowly until rising again at the end of the day, thus following the classical U-shape (Jain \& Joh 1988; Admati \& Pfleiderer 1988). Gao et al. (2018) looked for intraday momentum on the US stock market, and their results show there is a significant relationship between first and last half-hour returns when predicting the latter. Interestingly, the estimator coefficient got even more vital during the 2008-09 financial crisis. Their data from the year 1993 to 2013 also show a U-shaped volume pattern. However, the average traded volume in the last half-hour is slightly higher than in the first one. Richards \& Willows (2019) researched the trading activity of individual investors in the UK. Interestingly, the results showed a W-shaped trading pattern with the highest activity in the first half-hour with smaller peaks in the middle and at the end of the day.

As we can see, market anomalies have been studied many times before, and the results of the studies can sometimes differ as the stock market is constantly evolving thanks to the development of new technologies and by receiving more attention from the public. We believe analysing the mentioned anomalies on recent data from the US stock market affected by the pandemic is currently missing in the literature, allowing us to obtain new interesting results.

### 2.2 Stock market literature related to COVID-19

Since the beginning of the pandemic, countless pieces of literature have been published regarding the COVID-19 pandemic and stock markets. Baker et al. (2020) provide supporting evidence based on newspaper articles that the pandemic was the driving factor of a very turbulent period on the US stock market in the early stages of the pandemic at the end of February through April 2020. Their results also claim that no other pandemic in history had such an impact on the US stock market.

Zhang et al. (2020) compared data from February and March 2020 to measure the effect the pandemic has had on the volatility of various stock market returns. Their results for the US showed that the standard deviation in February was at 0.0069 and almost quadrupled to 0.0268 in March, the highest increase in volatility levels among the measured stock markets. Onali (2020) studied the impact of COVID-19 cases and deaths in the US and other six countries majorly affected by the pandemic on the US stock market returns.

Only the numbers reported in China showed a significant impact on the US market returns using the GARCH model. Uddin et al. (2021) used data from 34 developed and emerging markets and found that various economic factors can reduce the magnitude of volatility in uncertain time like a global pandemic.

Smales (2021) utilised google search volume for the "coronavirus" keyword as a proxy for investor attention to measure its correlation with stock returns. His results showed a significant negative relationship. The peak of coronavirus search volume in the US happened one day before S\&P 500 dipped to its lowest level during the pandemic. Okorie \& Lin (2021) employed the martingale difference spectral test to evaluate the adaptive Efficient Market Hypothesis (EMH) and found no substantial change in the level of information efficiency for the US stock market.

The majority of studies only focus on the whole US stock market by taking data from either S\&P 500 or DJIA indices. There are not many studies illustrating the impact across different industries of the market. However, Baek et al. (2020) took a closer look into the industry-level impact of COVID-19 on the idiosyncratic and systematic risk by utilising Markov switching regime model. Their results show a significant increase of total and idiosyncratic risk across all 30 examined industries. An increase in systematic risk is present for telecommunications or utilities, while industries such as automobiles and business equipment experienced a decrease in systematic risk. Just \& Echaust (2020) also used Markov switching approach to determine the relationship between S\&P 500 returns and various market indicators during the pandemic. Their results show close dependence between returns and both implied volatility and implied correlation. Choi (2021) tested the EMH by applying multifractal detrended fluctuation analysis on US stock market's individual sectors, his finding shows highest efficiency for the consumer discretionary sector and lowest for the utilities sector during the pandemic crash.

### 2.3 Hypotheses

We believe a closer look at the day of the week effect during the COVID-19 pandemic is missing in the current literature. It can be highly valuable as the market's dynamic was primarily affected by the uncertainty of the evolving situation and the constant inflow of both good and bad news. Possible patterns that might arise from the results would greatly benefit investors' decisions for future crashes on the stock market.

As we analyse three different periods, in two of which the market experienced strong growth and one that saw the S\&P 500 tumble by more than a third in a matter of days, it will be interesting to see the development of day of the week effect both in terms of average returns and volatility. We believe that we will see the Monday effect being the most significant in all cases. However, we expect a strongly negative relationship for the crash period instead of a positive one for the bull period, as the inflow of bad news regarding the pandemic development will cause investors to sell largely on Mondays. The other scenario is the one closer to the EMH and more specifically to the assumption stating, that investors are rational and always take the right decision (Fama 1970), which would suggest investors realising this weekend development beforehand and reflecting it on Friday returns, thus negating the Monday effect. We expect the day of the week effects in terms of returns to be the same for all eleven sectors of the S\&P 500 across all periods.

In terms of volatility, we anticipate more interesting cross-sector results. We expect volatility increase mainly for Information Technology, Health Care and Financials sectors. In contrast, Consumer Staples or Utilities sectors should not be much affected as the included companies mainly profit from necessities. The overall market volatility during the crash period will undoubtedly increase.

We also believe investigating the intraday volume patterns will bring significant results even with a small number of observations. Historically, we can see a heavily U-shaped trading pattern in terms of volume during the day. It is believed to be caused mainly due to all earnings and significant macroeconomic news being released before the market opens, causing this information to be processed heavily during the first 30 minutes of trading, after which the market cools off (Gao et al. 2018). While on the other end of the day, institutional traders put enormous emphasis on closing prices as they use them to calculate portfolio returns and other various financial indicators. At the same time, market makers often want to avoid overnight risk and close their positions (Cushing \& Madhavan 2000). However, during the COVID-19 pandemic bear market, these factors probably did not play such a significant role. We expect flattening of the U-shape curve and mid-day trading volumes accounting for more of the overall daily volume.

## Chapter 3

## Data

This section will cover information about the data used in the research. We will also outline the time periods for the proposed analysis. We want to understand how certain behaviours changed in response to the pandemic directly and in the period after the crash when the market started rising again.

The information and data from Section 3.1 were obtained from S\&P Global wesbite ${ }^{1}$. The data for second part of our analysis mentioned in Section 3.2 were downloaded from Dukascopy ${ }^{2}$.

### 3.1 Standard and Poor's 500 index (S\&P 500)

As we analyse the effect on the US stock market, the S\&P 500 is an excellent representation of the whole market. The index comprises 500 leading US companies on the stock market, and it covers approximately $80 \%$ of available market capitalisation. This indicator's history goes back to 1957, when it was created as the first US market-cap-weighted stock market index. In 2005, the calculation of the index was changed to float-adjusted market-cap-weighted index, which better reflects the value being traded by investors as only so-called free-float ${ }^{3}$ shares are weighted in, meaning that the weight of each stock is calculated based on the following formula:

$$
\text { Weight }_{i}=\frac{\text { Float Adjusted Market Cap }{ }_{i}}{\sum_{n=1}^{500} \text { Float Adjusted Market Cap }}
$$

[^1]Our analysis will be working with the more common price return version of the S\&P 500 index, which only reflects the stock prices, excluding the paid out dividends. We downloaded daily close index values from the beginning of 2018 until March 15, 2021. In our model we are working with dummy variables focusing on three different periods outlined as follows:

1. Before: Starting from the earliest observation of the dataset on January 2, 2018, until January 31, 2020, when the Trump administration declared a public health emergency.
2. During: The main pandemic crash period after the declared emergency with first observation on February 3, 2020 until March 20, 2020, when massive QE with positive effect got announced the weekend after the last observation.
3. After: Period largely affected by endless QE from March 23, 2020 to March 15, 2021.

Figure 3.1: S\&P 500 daily index values, main index and top 5 sectors


Figure 3.2: S\&P 500 daily index values, bottom 6 sectors


- FIN - ENRG -RE
- MAT - UTIL -CMS


### 3.1.1 Sectoral breakdown of the S\&P 500 index

The 500 stocks included in the S\&P 500 are broken down into 11 different sectors. The first part of our analysis is conducted on all of the 11 sectors as well as the S\&P 500, to be able to measure the impact on each part of the economy.

The obtained datasets are graphically visualized in Figure 3.1 and Figure 3.2 with different periods outlined by the dotted line.

In the following part, we will give a brief description of the sectors and list the top 5 constituents by index weight for each of them (as of this thesis's writing) (S\&P Global 2021). A broad understanding of the differences between specific sectors is crucial in interpreting the results in our analysis.

## Information Technology - IT

The Information Technology sector includes 76 companies that offer software and information technology consulting, data processing, and also manufacturers and distributors of technology hardware and equipment such as cell phones, computers, semiconductors etc...

Top 5 constituents: Apple Inc. (AAPL), Microsoft Corp (MSFT), Visa Inc A (V), Nvidia Corp (NVDA), Mastercard Inc A (MA)

## Health Care - HC

A total of 63 constituents in the Health Care sector, such as healthcare services and providers, manufacturers of healthcare equipment and supplies, technology companies related to healthcare, and biotechnology and pharmaceutical companies.

Top 5 constituents: Johnson \& Johnson (JNJ), Unitedhealth Group Inc (UNH), Abbott Laboratories (ABT), AbbVie Inc. (ABBV), Pfizer Inc (PFE)

## Consumer Discretionary - CD

This sector includes 61 companies closely operating in the retail sector, such as automobile manufacturers, household durables, leisure equipment or apparel stores. Hotels, restaurants and other leisure facilities are also included.

Top 5 constituents: Amazon.com Inc (AMZN), Tesla Inc (TSLA), Home Depot Inc (HD), Nike Inc B (NKE), McDonald's Corp (MCD)

## Industrials - IND

The Industrials sector is comprised of 73 businesses that manufacture and distribute capital goods such as machinery, electrical equipment, building products, aircraft and defence. The sector also includes commercial services providers such as construction and engineering, printing, logistics, human resources, or consulting services.

Top 5 constituents: Honeywell Intl Inc (HON), Union Pacific Corp (UNP), Caterpillar Inc (CAT), United Parcel Service Inc B (UPS), Boeing Co (BA)

## Consumer Staples - CS

Consumer staples sector is similarly focused on retail as the Consumer Discretionary sector, however, this sector includes 32 companies that produce more non-durable goods such as manufacturers and distributors of food and beverages, tobacco, non-durable household goods and personal products.

Top 5 constituents: Walmart Inc (WMT), Procter \& Gamble Co (PG), Cocacola Co (KO), Pepsico Inc (PEP), Costco Wholesale Corp (COST)

## Financials - FIN

The Financials sector consists of 65 businesses such as banks, thrifts, insurance companies, brokers, asset management companies and other types of businesses closely tied to finances.

Top 5 constituents: Berkshire Hathaway B (BRK.B), JP Morgan Chase \& Co (JPM), Bank of America Corp (BAC), Wells Fargo \& Co (WFC), Citigroup Inc (C)

## Materials - MAT

This sector includes 28 companies that manufacture construction materials, glass, paper, chemicals, forest products, packaging products. Mining companies and producers of steel are also included.

Top 5 constituents: Sherwin-Williams Co (SHW), Ecolab Inc (ECL), Air Products \& Chemicals Inc (APD), Freeport-McMoran Inc (FCX), Newmont Corporation (NEM)

## Energy - ENRG

The Energy sector includes 23 companies operating in exploration, production, refining, storage and transportation of oil and gas, coal and consumable fuels.

Top 5 constituents: Exxon Mobil Corporation (XOM), Chevron Corporation (CVX), ConocoPhilips (COP), EOG Resources Inc (EOG), Schlumberger Limited (SLB)

## Utilities - UTIL

The Utilities sector includes 28 companies such as gas, electric and water utilities, and independent power producers and energy traders. The sector also includes companies that generate and distribute electricity obtained from renewable resources.

Top 5 constituents: Nextera Energy Inc (NEE), Duke Energy Corp (DUK), Southern Co. (SO), Dominion Energy Inc (D), Sempra Energy (SRE)

## Real Estate - RE

This sector includes 30 companies active in the development and management of real estate as well as equity real estate investment trusts (REITs), however, mortgage REITs are included in the Financials sector.

Top 5 constituents: American Tower Corp (AMT), Prologic Inc (PLD), Crown Castle International Corp (CCI), Equinix Inc (EQIX), Public Storage (PSA)

## Communication Services - CMS

Communications services sector includes 26 companies that provide content such as entertainment, news and social media primarily on the internet, also includes providers of internet, broadband, cellular, cable and landlines.

Top 5 constituents: Alphabet Inc Class C/A (GOOG/GOOGL), Facebook Inc (FB), Walt Disney Company (DIS), Comcast Corp (CMCSA), Verizon Communications (VZ)

### 3.2 USA500 intraday data

For the intraday volume analysis, we obtained 30-minute data from Dukascopy. The downloaded index is called USA500, and according to the methodology provided on the website, it includes top 500 stocks on the US stock market. We could not use high-frequency data of the S\&P 500 as the index is not directly traded on the stock market and providers who recalculate the data typically charge high fees for their datasets. However, the index values are almost identical to the S\&P 500 as they should include the same companies. The correlation of daily close prices between the USA500 and S\&P 500 is 0.999992 .

The observed period for the analysis includes data from January 1, 2019, to February 26, 2021. The downloaded dataset was continuous and included premarket ${ }^{4}$ trading hours and non-trading hours during weekends and holidays. To clean the dataset of such observations, we first excluded all observations outside the regular trading hours of the major US stock exchanges between 9:30 a.m. and 4:00 p.m. EST. After dropping weekend and holiday observations, we still had to exclude shortened trading days as those observations would influence

[^2]our results due to the trading days not lasting the entire 6.5 hours. A list of all excluded holidays and shortened trading days can be found in Table A.2.

For this analysis, we divided the observed timeline into three periods similarly as in the previous section:

1. Before: Starting from the earliest observation of the dataset on January 2, 2019, until January 31, 2020, when the Trump administration declared a public health emergency.
2. During: The main pandemic crash period after the declared emergency with first observation on February 3, 2020, until March 20, 2020, when massive QE with positive effect got announced the weekend after the last observation.
3. After: Period largely affected by endless QE from March 23, 2020 to February 26, 2021.

Table 3.1: Summary statistics of volume traded of the USA 500 index, in millions

|  | Before |  | During |  | After |  |
| ---: | ---: | :--- | :--- | :--- | :--- | :--- |
| half hour | mean | STD | mean | STD | mean | STD |
| 1 | 5.04 | $(3.01)$ | 12.80 | $(10.81)$ | 12.30 | $(6.75)$ |
| 2 | 3.77 | $(2.48)$ | 12.87 | $(13.05)$ | 9.87 | $(6.23)$ |
| 3 | 3.03 | $(1.99)$ | 11.06 | $(11.25)$ | 8.90 | $(6.38)$ |
| 4 | 2.68 | $(2.09)$ | 10.65 | $(11.04)$ | 7.98 | $(6.12)$ |
| 5 | 2.35 | $(1.79)$ | 10.20 | $(11.41)$ | 6.84 | $(5.37)$ |
| 6 | 1.89 | $(1.50)$ | 10.65 | $(10.98)$ | 6.17 | $(5.24)$ |
| 7 | 1.64 | $(1.41)$ | 9.96 | $(11.35)$ | 5.65 | $(5.11)$ |
| 8 | 1.52 | $(1.42)$ | 10.09 | $(11.83)$ | 5.37 | $(5.12)$ |
| 9 | 1.52 | $(1.60)$ | 10.43 | $(11.90)$ | 5.23 | $(4.88)$ |
| 10 | 1.83 | $(1.87)$ | 10.53 | $(11.46)$ | 6.27 | $(5.15)$ |
| 11 | 1.83 | $(2.09)$ | 10.91 | $(12.28)$ | 6.37 | $(5.41)$ |
| 12 | 1.94 | $(1.98)$ | 10.62 | $(12.27)$ | 7.47 | $(5.79)$ |
| 13 | 2.84 | $(2.06)$ | 12.61 | $(14.26)$ | 9.59 | $(6.34)$ |

## Chapter 4

## Methodology

This section's main objective is to provide sufficient theoretical background into topics relevant for our analysis. Namely, we will introduce conditional heteroscedastic models that will be used in the empirical research and the methodology about how to find the best fit of the model. We will also cover the Analysis of variance (ANOVA) method, which we use to test the statistical significance of changes in the intraday volume patterns during the pandemic. For this chapter's purpose, two well-acknowledged books by Tsay (2005) and Bartoszyński \& Niewiadomska-Bugaj (2008) were used to provide the necessary theory behind the subjects.

### 4.1 Financial time series analysis

### 4.1.1 Stationarity

When performing a time series analysis, it is important to have stationary data as many models and statistical tools rely on its implications of timeinvariant properties. For this analysis, it is sufficient to understand only the weak stationarity as the strict one is hard to verify empirically and not needed for the models used. A time series $\left\{r_{t}\right\}$ is weakly stationary when $E\left(r_{t}\right)=\mu$ is constant for all observations and $\operatorname{Cov}\left(r_{t}, r_{t-\ell}\right)=\gamma_{\ell}$ only depends on $\ell$, which is an arbitrary integer.

### 4.1.2 Return series

The stationarity assumption has an important implication for financial time series analysis, as we are working with data where the weak stationarity rarely
holds true. From Figure 3.1 we can see that expected value is very likely to be time-varying for our time series. To overcome this fact we will use the return series, and more specifically the log return series $\left\{r_{t}\right\}$ as its statistical properties are more tractable:

$$
\begin{equation*}
r_{t}=\ln \frac{P_{t}}{P_{t-1}}=\ln \left(P_{t}\right)-\ln \left(P_{t-1}\right) \tag{4.1}
\end{equation*}
$$

Where $P_{t}$ stands for the price of the stock at time $t$, in our case the index points value.

### 4.1.3 ADF test

For testing whether the return series $\left\{r_{t}\right\}$ is stationary, we will be using the Augmented version of the Dickey-Fuller test (Dickey \& Fuller 1979). Suppose we have the following model:

$$
r_{t}=\alpha_{0}+\alpha r_{t-1}+\phi_{1} \Delta r_{t-1}+\ldots+\phi_{L} \Delta r_{t-L}+\epsilon_{t}
$$

Where $\alpha_{0}$ is a constant, $\epsilon_{t}$ is an error term, $\Delta r_{t-\ell}$ is the first difference at lag $\ell$ and $\alpha, \phi_{\ell}$ are estimated coefficients.

In the ADF test, we are testing whether there is a unit root process present. Thus the null hypothesis assumes that $\alpha=1$. Ultimately we want to reject the null hypothesis, accepting the alternative one meaning the return series is stationary.

### 4.1.4 KPSS test

Another way to test for stationarity in our data is the KPSS test, the name of the test comes from the initials of Kwiatkowski, Phillips, Schmidt, \& Shin (1992). Suppose the following model for our return series $\left\{r_{t}\right\}$ :

$$
r_{t}=\beta_{t}+d_{t}+\epsilon_{t}, \quad d_{t}=d_{t-1}+u_{t}
$$

Where we have deterministic trend $\beta_{1}$, random walk $d_{t}$, stationary error $\epsilon_{t}$ and $u_{t}$ are normal independent and identically distributed (iid) variables with a zero mean and variance $\sigma_{u}^{2}$. The initial value of $d_{0}$ is fixed intercept.

Unlike the ADF test, here we have the null hypothesis $H_{0}: \sigma_{u}^{2}=0$ stating that the series is stationary against the alternative one $H_{1}: \sigma_{u}^{2} \neq 0$, which
assumes unit root presence. In the analysis, we will be using both the ADF and the KPSS test, which will derive more powerful results.

### 4.1.5 Auto-correlation function

When working with a weakly stationary return series $\left\{r_{t}\right\}$ the Autocorrelation Function (ACF) is a great first indicator of the series's behaviour and will help us find the right order of moving-average part of the Autoregressive MovingAverage (ARMA) model which we will introduce later in this section. The correlation coefficient between $r_{t}$ and $r_{t-\ell}$ under a weak stationarity assumption is a function of $\ell$ only and we call it the lag- $\ell$ autocorrelation of $r_{t}$ denoted as $\rho_{\ell}$ :

$$
\rho_{\ell}=\frac{\operatorname{Cov}\left(r_{t}, r_{t-\ell}\right)}{\sqrt{\operatorname{Var}\left(r_{t}\right) \operatorname{Var}\left(r_{t-\ell}\right)}}=\frac{\operatorname{Cov}\left(r_{t}, r_{t-\ell}\right)}{\operatorname{Var}\left(r_{t}\right)}=\frac{\gamma_{\ell}}{\gamma_{0}}
$$

Where we used the property of weakly stationary time series $\left\{r_{t}\right\}$ that $\operatorname{Var}\left(r_{t}\right)=$ $\operatorname{Var}\left(r_{t-\ell}\right)$. If $\rho_{\ell}=0$ for all $\ell>0$, we can say that a weakly stationary time series is not serially correlated.

### 4.1.6 Partial auto-correlation function

The Partial Autocorrelation Function (PACF) is a great tool for determining the right order of autoregressive part of the ARMA model. Unlike the ACF, the PACF estimates the coefficients while taking into account lower lag orders of the PACF. An effective way to describe this is to consider the following Autoregressive models:

$$
\begin{aligned}
r_{t} & =\phi_{0,1}+\phi_{1,1} r_{t-1}+e_{1 t} \\
r_{t} & =\phi_{0,2}+\phi_{1,2} r_{t-1}+\phi_{2,2} r_{t-2}+e_{2 t} \\
r_{t} & =\phi_{0,3}+\phi_{1,3} r_{t-1}+\phi_{2,3} r_{t-2}+\phi_{3,3} r_{t-3}+e_{3 t}
\end{aligned}
$$

$$
\vdots \quad \vdots
$$

Where $\phi_{0, j}$ is a constant term, $\phi_{i, j}$ is the coefficient of $r_{t-i}$ and $\left\{e_{j t}\right\}$ is the error term of an $\operatorname{AR}(\mathrm{j})$ model. These models can be estimated using the least squares method, the estimates of $\phi_{\ell, \ell}$ are then the lag - $\ell$ sample PACF of $r_{t}$.

### 4.1.7 Portmanteau statistic and Ljung-Box test

In financial econometrics it is important and often required to test jointly, whether several autocorrelations of $r_{t}$ are equal to 0 to show if there is a dependence in the return series or not. Box \& Pierce (1970) proposed the Portmanteau test statistic denoted as $Q^{*}(m)$ for the null hypothesis $H_{0}: \rho_{1}=$ $\ldots=\rho_{m}=0$, in words if the series is independent, against $H_{1}: \rho_{i} \neq 0$ for $i \in\{1, \ldots, m\}$ suggesting dependant series. Under the assumption that $\left\{r_{t}\right\}$ is an iid sequence, $Q^{*}(m)$ is assymptotically a chi-squared random variable with $m$ degrees of freedom.

$$
Q^{*}(m)=T \sum_{\ell=1}^{m} \hat{\rho}_{\ell}^{2}
$$

T is the number of observations in the sample and $\hat{\rho}_{\ell}$ is a biased estimator of $\rho_{\ell}$, where the bias is in the order of $1 / T$, which in our case is minimal, as we have over 800 observations for our return series.

Ljung \& Box (1978) modified the Portmanteau statistic to increase the power of of the test in finite samples.

$$
Q(m)=T(T+2) \sum_{\ell=1}^{m} \frac{\hat{\rho}_{\ell}^{2}}{T-\ell}
$$

In our empirical research we will be using this modified version to jointly test for several autocorrelations. The selection of $m$ can affect the performance of the $Q(m)$ statistic heavily, we will be sticking to the suggested (Tsay 2005) $m \approx \ln (T)$ which in our case is $\ln (805) \approx 7$.

### 4.1.8 ARMA model

After finding some dependancy in our dataset, we can employ the ARMA model to predict $\left\{r_{t}\right\}$. ARMA is a combination of Autoregressive (AR) model and Moving-Average (MA) model, which together create a more complex model, so that the number of parameters are kept small. A general ARMA(p,q) is defined in the form:

$$
\begin{equation*}
r_{t}=\phi_{0}+\sum_{i=1}^{p} \phi_{i} r_{t-i}+\sum_{i=1}^{q} \theta_{i} a_{t-i}+a_{t} \tag{4.2}
\end{equation*}
$$

Where $\phi_{0}+\sum_{i=1}^{p} \phi_{i} r_{t-i}$ is the auto-regressive part of the model, and $\sum_{i=1}^{q} \theta_{i} a_{t-i}$ is the moving-average part. $\left\{a_{t}\right\}$ are white noise residuals, $\phi_{0}$ is constant, $\phi_{i}$ and $\beta_{i}$ are the estimated coefficients of the AR and MA processes, respectively.

However, the ARMA model is rarely used for forecasting future values in
financial time series, as it is relying on knowing the present $(\mathrm{t})$ value of $\left\{a_{t}\right\}$. Under the assumption that $\left\{a_{t}\right\}$ is a white noise series, meaning it is a sequence of iid random variables with finite mean and variance, the ARMA model is perhaps the most reliable estimate. However, in the case of financial time series, $\left\{a_{t}\right\}$ is rarely a white noise series, as the residuals hardly ever follow a normal distribution. What we observe in financial time series, and especially in stock prices, is so-called volatility clustering, firstly noted by Mandelbrot (1963). Volatility clustering suggests that in times of high price variation, the price variation is expected to stay high, and vice versa.

### 4.1.9 Conditional heteroscedastic models

The problem with volatility modelling is that it is not directly observable. In our case of daily log returns of the S\&P 500 indices, we only have one observation in a trading day. We would need high-frequency data for more consistent estimates of volatility, which is often harder to obtain from publicly available sources, especially for stock indices. However, in our analysis, the daily returns should be sufficient if we apply the correct conditional heteroscedastic models.

When studying volatility, it is important to assume that the series $\left\{r_{t}\right\}$ is either serially uncorrelated or with minor lower order serial correlations, but it is dependant. We will also consider the conditional mean and conditional variance of $\left\{r_{t}\right\}$ given $F_{t-1}$ :

$$
\begin{equation*}
\mu_{t}=E\left(r_{t} \mid F_{t-1}\right), \quad \sigma_{t}^{2}=\operatorname{Var}\left(r_{t} \mid F_{t-1}\right)=E\left[\left(r_{t}-\mu_{t}\right)^{2} \mid F_{t-1}\right] \tag{4.3}
\end{equation*}
$$

Where $F_{t-1}$ denotes the information set available at time $t-1$. In conditional heteroscedastic models, we still assume ARMA( $\mathrm{p}, \mathrm{q}$ ) model for the mean $\mu_{t}$, however we take away the series $\left\{a_{t}\right\}$, which will be modeled seperately by the conditional heteroscedasticity models. We can see this in the following equations.

$$
\begin{equation*}
r_{t}=\mu_{t}+a_{t}, \quad \mu_{t}=\phi_{0}+\sum_{i=1}^{p} \phi_{i} r_{t-i}+\sum_{i=1}^{q} \theta_{i} a_{t-i} \tag{4.4}
\end{equation*}
$$

When combining equations (4.3) and (4.4) we derive

$$
\sigma^{2}=\operatorname{Var}\left(r_{t} \mid F_{t-1}\right)=\operatorname{Var}\left(a_{t} \mid F_{t-1}\right)
$$

The models which we will introduce next are concerned with the evolution of $\sigma_{t}^{2}$ over time.

### 4.1.10 ARCH

Autoregressive Conditional Heteroscedasticity (ARCH) model, developed by Engle (1982), is the first model that allows for systematic modelling of volatility in financial time series. General ARCH(m) model assumes that

$$
\begin{equation*}
a_{t}=\sigma_{t} \epsilon_{t}, \quad \sigma_{t}^{2}=\alpha_{0}+\alpha_{1} a_{t-1}^{2}+\ldots+\alpha_{m} a_{t-m}^{2}, \tag{4.5}
\end{equation*}
$$

where $\left\{\epsilon_{t}\right\}$ is a sequence of iid random variables with zero mean and variance equal to $1, \alpha_{0}>0$, and $\alpha_{i} \geq 0$ for $i>0$. The coefficients $\alpha_{i}$ must satisfy some regularity conditions in order to obtain finite unconditional variance of $a_{t}$.

From the model specification, we can see that large past squared shocks $\left\{a_{t-i}^{2}\right\}$ imply a large conditional variance $\sigma_{t}^{2}$ for $a_{t}$, which in practice suggests that large shocks are expected to be followed by another large shock. Thus ARCH model is a great tool for modelling volatility of stock price returns, where we can observe volatility clustering.

One of the weaknesses of ARCH model is that it is very mechanical way to describe the behavior of the conditional variance. It does not provide us with any insights for understanding the source of variations of a financial time series. The model also assumes that positive and negative shocks have the same effect on volatility. In practice, financial time series often respond differently to positive and negative shocks.

### 4.1.11 GARCH

The simplicity of ARCH model can sometimes lead to high amount of parameters needed for quality description of the volatility. Bollerslev (1986) proposes an extension of the model known as Generalized Autoregressive Conditional Heteroscedasticity (GARCH) model. A mean corrected log return series $a_{t}$ follows a $\operatorname{GARCH}(\mathrm{m}, \mathrm{s})$ model if

$$
\begin{equation*}
a_{t}=\sigma_{t} \epsilon_{t}, \quad \sigma_{t}^{2}=\alpha_{0}+\sum_{i=1}^{m} \alpha_{i} a_{t-i}^{2}+\sum_{j=1}^{s} \beta_{j} \sigma_{t-j}^{2}, \tag{4.6}
\end{equation*}
$$

where $\left\{\epsilon_{t}\right\}$ is a sequence of iid random variables with zero mean and variance equal to $1, \alpha_{0}>0$, and $\alpha_{i} \geq 0, \beta_{j} \geq 0$ and $\sum_{i=1}^{\max (m, s)}\left(\alpha_{i}+\beta_{i}\right)<1$, which implies that the unconditional variance of $a_{t}$ is finite, whereas the conditional variance of $\sigma_{t}^{2}$ is evolving over time. We can see that equation (4.6) reduces
down to (4.5) when parameter $s=0$. Also if $m=s=0,\left\{a_{t}\right\}$ is only white noise and we cannot observe any ARCH effect.

The difference between ARCH and GARCH is that the latter allows for lagged conditional variances $\sigma_{t-j}^{2}$ to enter the model as visible from the equation (4.6). Consequently, this leads to more simple models, where we often find that $\operatorname{GARCH}(1,1)$ is the best fit. We will explain more about finding the best model fit in Subsection 4.1.13.

### 4.1.12 T-GARCH

We often find asymmetries in financial time series data, and as we already mentioned, markets tend to react differently to positive and negative shocks. The standard ARCH and GARCH models have no tool to deal with that. Zakoian (1994) proposed an implementation that can deal with asymmetry, the threshold GARCH model (TGARCH). TGARCH ( $\mathrm{m}, \mathrm{s}$ ) model that we will be using in our empirical research is defined as follows:

$$
\begin{equation*}
a_{t}=\sigma_{t} \epsilon_{t}, \quad \sigma_{t}=\alpha_{0}+\sum_{i=1}^{m} \alpha_{i} \sigma_{t-i}\left(\left|a_{t-i}\right|-\eta_{i} a_{t-i}\right)+\sum_{j=1}^{s} \beta_{j} \sigma_{t-j}, \tag{4.7}
\end{equation*}
$$

where $\eta_{i}$ is the coefficient in the leverage term and $\left|\eta_{i}\right| \leq 1$. We should also note that in the case of TGARCH, we are modelling $\sigma_{t}$ instead of $\sigma_{t}^{2}$. This is a key difference to the earlier proposed threshold model known as GJR-GARCH (Glosten et al. 1993). Modelling conditional standard deviation instead of conditional variance allows us to have no positivity constraints. This is especially useful when adding dummy variables to the model, which will be a key part of the empirical analysis, as the coefficients can turn out negative, telling us additional information.

### 4.1.13 Model fitting based in information criteria

When working with conditional heteroscedasticity models, it is crucial to specify the model correctly, both for conditional mean and variance. In our empirical research we will be minimising the information criteria to determine the best number of parameters in our model. All information criteria are likelihood based. We will be using the Akaike Information Criterion (Akaike 1973) defined as

$$
\begin{equation*}
A I C=-2 \ln (\hat{L})+2 k \tag{4.8}
\end{equation*}
$$

Where $\hat{L}$ is the likelihood function evaluated at the maximum likelihood estimates and k is the number of estimated parameters in the model.

### 4.2 Intraday volume analysis

### 4.2.1 Daily volume traded in percentage

In the analysis of the daily volume patterns on the US stock market during the COVID-19 pandemic crash, we are interested in the pattern changes in percentage volumes rather than absolute volumes. While it is pretty apparent that the volume of trades increased during the big sellout on the market, it is not so clear whether the proportion of trades in a given day changed significantly. Thus we will use the following formula to transform our absolute volume data into proportionate volume data.

$$
\begin{equation*}
P_{i d}=\frac{V_{i d}}{\sum_{j=1}^{13} V_{j d}} \tag{4.9}
\end{equation*}
$$

Where $V_{i d}$ is the volume traded on day $d$ in half-hour $i \in\{1, \ldots, 13\}$. From this formula, we can see that $\sum_{i=1}^{13} P_{i d}$ must equal 1.

### 4.2.2 ANOVA

ANOVA is a great tool for testing whether means across multiple groups differ significantly. The main objective is to test

$$
H_{0}: \mu_{1}=\mu_{2}=\ldots=\mu_{k} \quad \text { against } \quad H_{1}: \mu_{i} \neq \mu_{i^{\prime}} \text { for some } i, i^{\prime}
$$

Suppose we have $k$ groups each with $n_{i}$ observations where $i \in\{1, \ldots, k\}$. Then first we calculate the sum of squares for between group variability:

$$
S S_{\text {between }}=n_{1}\left(\bar{X}_{1}-\bar{X}_{G}\right)^{2}+\ldots+n_{k}\left(\bar{X}_{k}-\bar{X}_{G}\right)^{2}
$$

Where $\bar{X}_{i}$ is the mean for group $i$ and $\bar{X}_{G}$ is the total mean across all groups. Then we can derive the mean square for between group variability:

$$
M S_{\text {between }}=\frac{S S_{\text {between }}}{k-1}
$$

Next part is to calculate the sum of squares for within group variability, from which we can obtain the mean square as well.

$$
\begin{gathered}
S S_{\text {within }}=\sum_{j=1}^{n_{1}}\left(x_{j 1}-\bar{X}_{1}\right)^{2}+\ldots+\sum_{j=1}^{n_{k}}\left(x_{j k}-\bar{X}_{k}\right)^{2} \\
M S_{\text {within }}=\frac{S S_{\text {within }}}{N-k}
\end{gathered}
$$

Where $\left\{x_{j i}\right\}$ are observations of group $i \in\{1, \ldots, k\}, j \in\left\{1, \ldots, n_{i}\right\}$, and $N$ stands for the total number of observations across all groups.

Lastly we calculate the F-test statistic. We reject the hypothesis $H_{0}: \mu_{1}=$ $\mu_{2}=\ldots=\mu_{k}$ at level of significance $\alpha$ if:

$$
F=\frac{M S_{\text {between }}}{M S_{\text {within }}}>F_{\alpha, k-1, N-k}
$$

It is important to note that in ANOVA, we always use a one-sided critical region since any violation of $H_{0}$ tends to increase the numerator of the F statistic without affecting the denominator.

## Chapter 5

## Empirical research and results

### 5.1 Descriptive statistics and return series

### 5.1.1 Log-return series and stationarity

We obtained the log-return data by following the Equation 4.1. In Figure 5.1 are plotted the log returns for each of the sectors. At first glance, we can see that the Consumer Staples and Health Care sectors have one of the lowest (but still pretty big) spikes during the pandemic market crash compared to other sectors. It implicates that those sectors were less affected by the pandemic. However, we will get much more precise results from the conditional heteroscedasticity models later in this chapter.

As mentioned in the methodology, the stationarity assumption is critical for working with time series data. We employed the ADF and the KPSS tests mentioned in the methodology to test for stationarity. The results in Table A. 1 show that the log-return series is stationary for all sectors.

### 5.1.2 Descriptive statistics

From the descriptive statistics in Table 5.1 we can immediately observe that the variance is relatively high compared to the mean, implicating volatile series, and especially for the Energy sector, which is the only sector that decreased over the observed period as we can see from the negative mean. The high volatility and decreasing trend for the Energy sector might be explained due to the increasing popularity of green fuels, which can repel investors from believing in the future of consumable fuels which dominate the Energy sector.

The negative skewness across all sectors implies the returns tend to generate

Figure 5.1: Daily log returns from 2018 to March 15, 2021


Table 5.1: Descriptive statistics of the S\&P 500 log returns

|  | N | Mean | Variance | Skewness | Kurtosis | Min | Max |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| SP500 | 805 | 0.00049 | 0.00021 | -1.02 | 19.02 | -0.128 | 0.090 |
| IT | 805 | 0.00093 | 0.00033 | -0.66 | 13.83 | -0.150 | 0.113 |
| HC | 805 | 0.00042 | 0.00018 | -0.48 | 13.19 | -0.105 | 0.073 |
| CD | 805 | 0.00067 | 0.00023 | -1.08 | 14.71 | -0.129 | 0.083 |
| IND | 805 | 0.00032 | 0.00028 | -0.70 | 14.88 | -0.122 | 0.120 |
| CS | 805 | 0.00018 | 0.00014 | -0.38 | 18.02 | -0.097 | 0.081 |
| FIN | 805 | 0.00026 | 0.00035 | -0.69 | 17.24 | -0.151 | 0.124 |
| MAT | 805 | 0.00033 | 0.00027 | -0.69 | 13.48 | -0.121 | 0.110 |
| ENRG | 805 | -0.00037 | 0.00060 | -1.03 | 18.88 | -0.224 | 0.151 |
| UTIL | 805 | 0.00022 | 0.00024 | -0.20 | 20.72 | -0.123 | 0.123 |
| RE | 805 | 0.00023 | 0.00027 | -1.74 | 26.83 | -0.181 | 0.083 |
| CMS | 805 | 0.00046 | 0.00023 | -0.69 | 11.10 | -0.110 | 0.088 |

primarily small positive returns. In contrast, the negative returns tend to be more extreme as the distribution's left-tail is longer. This is also visible from the minimum values being greater than the maximum values in absolute terms. High positive kurtosis is an indicator of heavy tails and more outliers in our series than we would find in a normal distribution.

### 5.2 S\&P 500 return series analysis

This section will be going through the steps mentioned in the methodology for the S\&P 500 index. The same steps will be applied to the individual sectors as well. However, we will not cover them separately and instead provide only the final results later in this chapter. Additional results for the individual sectors can be found in Appendix.

### 5.2.1 ARMA model

From the ACF in Figure 5.2 it is clear that there is a heavy autocorrelation structure in the returns. This should not be the case under the EMH, however, our data is heavily affected by the pandemic period, so we may observe some inefficiencies in terms of linear dependency. When computing the Ljung-Box test for seven lags, we can easily reject the null hypothesis as the p-value is lower than $2.2 * 10^{-16}$. Thus we accept the alternative hypothesis that there is dependence in the data. The PACF also shows a significant result for the first lag. From both the ACF and PACF, we can expect both the autoregressive and moving-average parts of the ARMA $(\mathrm{p}, \mathrm{q})$ model to be present, meaning that neither p nor q will equal 0 .

Figure 5.2: ACF and PACF of S\&P 500 daily log returns


Before moving on to minimising the information criteria and finding the correct $\operatorname{ARMA}(\mathrm{p}, \mathrm{q})$, we need to introduce the dummy variables, that will be included in the model. The dummy variables can result in different estimates of the ARMA ( $\mathrm{p}, \mathrm{q}$ ) and it is crucial to include them beforehand. The ARMA( $\mathrm{p}, \mathrm{q}$ ) model for the return series $\left\{r_{t}\right\}$ is defined as:

$$
\begin{align*}
& r_{t}=\phi_{0}+\sum_{i=1}^{p} \phi_{i} r_{t-i}+\sum_{i=1}^{q} \theta_{i} a_{t-i}+a_{t}+\gamma_{1} I_{D U R * M o n}+\gamma_{2} I_{A F T R * M o n}+  \tag{5.1}\\
& +\gamma_{3} I_{D U R * F r i} \gamma_{4} I_{A F T R * F r i}+\gamma_{5} D_{M o n}+\gamma_{6} D_{F r i}+\gamma_{7} D_{D U R}+\gamma_{8} D_{A F T R}
\end{align*}
$$

Where $I$ are interaction dummy variables, which equal 1 when both dummies are satisfied, i.e. $I_{D U R * M o n}$ equals 1 on Mondays in period During outlined in Section 3.1. $D$ dummy variables equal 1 when only the one condition in the index is satisfied. The rest of the equation is the same as in Equation 4.6.

Dummy variables for other days of the week than Monday and Friday are not included as this analysis's main interest is to observe the behaviour around weekends. From the existing literature, it is also apparent that Mondays and Fridays have had the most significant effects on the stock market. Given the low amount of observations in the analysis's focused periods, it is better not to over-parametrise the model.

After minimising the information criteria, the best fit of the model is ARMA $(3,1)$ with no intercept. However, the results shown in Table 5.2 do not follow the results from the autocorrelation function. We see that a sizeable moving-average coefficient cancels out the autoregressive coefficients, meaning that if there is an unexpected return of $1 \%$, the AR coefficients will expect the next day to return to be about $-1 \%$. In contrast, the MA coefficient will negate the shock by adding back the unexpected return of $1 \%$. Thus the results are hardly telling us any information. To obtain results easier to interpret, we will only optimise the $\mathrm{AR}(\mathrm{p})$ model with a maximum value of p up to 5 instead. The best model fit for the return series is $\operatorname{AR}(4)$ model with results shown in Table 5.2. We decided to include an intercept in the model to get rid of some potential linear trend in the series. The $\mathrm{AR}(4)$ model results are more in line with the autocorrelation function and will be easier to interpret. Also, the information criterion has changed marginally, meaning the likelihood of both models is very close. However, we will not be elaborating on the estimated coefficients of the ARMA models as the conditional heteroscedastic models will change those estimates once we account for the volatility modelling.

Table 5.2: ARMA models of the S\&P 500

|  | ARMA(3,1) |  | ARMA $(4,0)$ |  |  |
| :--- | ---: | ---: | ---: | ---: | :---: |
| $\phi_{0}$ | - | - | 0.0006 | $(0.001)$ |  |
| $\phi_{1}$ | -1.1269 | $(0.041)$ | -0.2614 | $(0.036)$ |  |
| $\phi_{2}$ | -0.0959 | $(0.053)$ | 0.1233 | $(0.037)$ |  |
| $\phi_{3}$ | 0.2087 | $(0.036)$ | 0.0223 | $(0.037)$ |  |
| $\phi_{4}$ | - | - | -0.1315 | $(0.035)$ |  |
| $\theta_{1}$ | 0.9160 | $(0.025)$ | - | - |  |
| $\gamma_{1}$ | -0.0084 | $(0.006)$ | -0.0094 | $(0.006)$ |  |
| $\gamma_{2}$ | 0.0053 | $(0.003)$ | 0.0057 | $(0.003)$ |  |
| $\gamma_{3}$ | -0.0089 | $(0.006)$ | -0.0057 | $(0.006)$ |  |
| $\gamma_{4}$ | -0.0014 | $(0.003)$ | -0.0017 | $(0.003)$ |  |
| $\gamma_{5}$ | -0.0007 | $(0.001)$ | -0.0011 | $(0.002)$ |  |
| $\gamma_{6}$ | 0.0005 | $(0.001)$ | -0.0003 | $(0.001)$ |  |
| $\gamma_{7}$ | -0.0071 | $(0.003)$ | -0.0076 | $(0.003)$ |  |
| $\gamma_{8}$ | 0.0016 | $(0.001)$ | 0.0010 | $(0.001)$ |  |
| AIC | -4667 |  | -4623 |  |  |

Note: Standard errors of estimates are in parenthesis.

### 5.2.2 ARCH effect

In methodology, we talked about the inefficiencies of using the ARMA model in financial time series. This subsection shows how that applies to our data before we move on to estimating the T-GARCH model. Figure 5.3 is an excellent visualisation of the fact that the AR model's fitted values are much less volatile than the actual values. This is because the autoregressive model does not estimate the disturbance $\left\{a_{t}\right\}$ and only assumes it is a white noise series.

Figure 5.3: Signal-noise ratio of the S\&P 500 daily log returns



However, some autocorrelation is still left in the data, as we can see from the ACF and PACF of the residuals in Figure 5.4. The fact that there is still some dependency in the residuals is essential. It means that the $\operatorname{AR}(4)$ is still leaving some information unused, and better results will be obtainable when employing conditional heteroscedastic models. If the residuals were just a white noise series, we would not observe any ARCH effect, and the AR model would probably be sufficient.

Figure 5.4: ACF and PACF of the S\&P 500 AR model fit residuals


To quickly test whether the data is suitable for applying ARCH models Engle (1982) proposed a way to measure for so-called ARCH effect in the data. The ARCH effect can be significantly approved by rejecting null hypothesis of homoscedastic residuals and accepting the alternative one of heteroscedastic residuals. One can measure the test by calculating the Portmanteau Q test statistic for squared residuals. In our case, we reject the null hypothesis as the Ljung-Box test at 7 lags returns p-value lower than $2.2 * 10^{-16}$. Concluding the presence of ARCH effect in the residuals, so we can move on to estimating the T-GARCH model.

### 5.2.3 T-GARCH model specification

We will be using the T-GARCH(m,s) model for estimating the volatility. We can see from the skewness in Table 5.1 there is a certain asymmetry in the data, so we think the Threshold GARCH model will be the best fit. It will allow us to find additional information regarding how significant the asymmetry is across sectors. For this analysis, the standard T-GARCH $(1,1)$ will be sufficient as the main focus is on comparing the data across sectors. Economists also often use variations of the standard $\operatorname{GARCH}(1,1)$ model as it is regarded satisfactory
with no need for higher orders of m or s when working with financial data (Brooks \& Burke 2003).

We will also be adding two dummy variables for measuring the volatility. Thus for the return series $\left\{r_{t}\right\}$ we will be using the following set of equations to estimate the T-GARCH $(1,1)$ :

$$
\begin{gather*}
r_{t}=\mu_{t}+a_{t}  \tag{5.2}\\
\mu_{t}=\phi_{0}+\sum_{i=1}^{p} \phi_{i} r_{t-i}+\gamma_{1} I_{D U R * M o n}+\gamma_{2} I_{A F T R * M o n}+\gamma_{3} I_{D U R * F r i}+  \tag{5.3}\\
+\gamma_{4} I_{A F T R * F r i}+\gamma_{5} D_{M o n}+\gamma_{6} D_{F r i}+\gamma_{7} D_{D U R}+\gamma_{8} D_{A F T R} \\
a_{t}=\sigma_{t} \epsilon_{t}  \tag{5.4}\\
\sigma_{t}=\alpha_{0}+\alpha_{1} \sigma_{t-1}\left(\left|a_{t-1}\right|-\eta_{1} a_{t-1}\right)+\beta_{1} \sigma_{t-1}+\delta_{1} D_{D U R}+\delta_{2} D_{A F T R} \tag{5.5}
\end{gather*}
$$

Where p equals 4 for the $\mathrm{S} \& \mathrm{P} 500$ return series, but different orders of p up to 5 will be used across sectors based on the information criterion minimisation. We added two dummy variables for the standard deviation equation. These will provide insight into the effects of the pandemic crash and the following period of quantitative easing brought on the market.

### 5.2.4 S\&P 500 T-GARCH results

In Table 5.3 are the estimated coefficients for the $\operatorname{T}-\operatorname{GARCH}(1,1)$ model with $\mathrm{AR}(4)$ as the included mean model. From the mean model results, the autoregressive coefficient $\phi_{1}$ is significant and slightly negative with an estimate of -0.071 . This result tells us that the market tends to contradict previous observation very slightly. If, for example, the market growths by $1 \%$ within a day, then the market is expected to return $-0.07 \%$ the next day based on the $\phi_{1}$ estimate. However, we still have to account for all of the other variables in the model.

Looking at the added dummy variables, we only obtained two significant results. The first one for $\gamma_{2}$ shows that the returns on Mondays in the period from March 23, 2020, onwards have been significantly higher. This is very interesting, and it shows that the calendar time hypothesis (French 1980) holds for this bull period on the US stock market. On the other hand, the Monday returns during the crash period $\left(\gamma_{1}\right)$ show a much stronger negative relationship than the Friday returns in the same period $\left(\gamma_{3}\right)$. Unfortunately, both of these results are statistically insignificant due to the low number of observations.

Table 5.3: S\&P 500 T-GARCH estimates

| Mean model results |  |  |  | STD model results |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :---: |
| $\phi_{0}$ | $7.4 \mathrm{E}--^{* *}$ | $(3.5 \mathrm{E}-4)$ | $\alpha_{0}$ | $0.0006^{* * *}$ | $(0.000)$ |  |
| $\phi_{1}$ | $-0.071^{* *}$ | $(0.034)$ | $\alpha_{1}$ | $0.153^{* * *}$ | $(0.033)$ |  |
| $\phi_{2}$ | 0.024 | $(0.034)$ | $\beta_{1}$ | $0.811^{* * *}$ | $(0.031)$ |  |
| $\phi_{3}$ | 0.018 | $(0.040)$ | $\eta_{1}$ | $0.875^{* * *}$ | $(0.198)$ |  |
| $\phi_{4}$ | -0.009 | $(0.034)$ | $\delta_{1}$ | 0.0007 | $(0.0006)$ |  |
| $\gamma_{1}$ | -0.0068 | $(0.0053)$ | $\delta_{2}$ | $0.0006^{* * *}$ | $(0.0001)$ |  |
| $\gamma_{2}$ | $0.0031^{* * *}$ | $(0.0009)$ |  |  |  |  |
| $\gamma_{3}$ | -0.0041 | $(0.0050)$ |  |  |  |  |
| $\gamma_{4}$ | -0.0004 | $(0.0019)$ |  |  |  |  |
| $\gamma_{5}$ | -0.0007 | $(0.0005)$ |  |  |  |  |
| $\gamma_{6}$ | 0.0004 | $(0.0007)$ |  |  |  |  |
| $\gamma_{7}$ | $0.0020^{* * *}$ | $(0.0007)$ |  |  |  |  |
| $\gamma_{8}$ | -0.0006 | $(0.0006)$ |  |  |  |  |
| Note: |  |  |  |  |  |  |
| nificance respectively. Standard errors of estimates are in |  |  |  |  |  |  |
| parenthesis |  |  |  |  |  |  |

However, we can still be reasonably confident that the Monday returns were lower when looking at the standard deviations. It confirms the hypothesis that investors did not prepare for the inflow of bad news during the weekends beforehand, resulting in lower returns on Mondays.

The second significant dummy $\gamma_{7}$ shows a positive relationship for the period during the crash. This is very interesting, as we would probably expect a negative relationship instead. This can be because many negative returns possibly happened on Mondays and Fridays during the crash, which coefficients still have much stronger negative relationship estimates. Alternatively, the negative returns are reflected in the mean and volatility model so well that we do not see a change of pattern, which would result in a significantly negative estimate of $\gamma_{7}$. Something similar is the case for the period after the crash as the estimate of $\gamma_{8}$ is negative and insignificant, though we would expect it to be positive and significant.

We also observe a positive significant intercept $\phi_{0}=0.00074$, showing that there is a positive trend in the series. It comes as no surprise, as the S\&P 500 has gained in value over the observed period.

From the volatility model, we can see a very significant intercept $\alpha_{0}$, which is not telling us much information on its own. However, when comparing it with the dummy variables $\delta_{1}$ and $\delta_{2}$, it is rather interesting as we can see that
the volatility doubled in the period after the crash, which also has a significant coefficient. For $\delta_{1}$, we can see something similar as in the mean model. While we know that the volatility during the crash increased dramatically, the observed period is too short, and the information is again mainly included in the T$\operatorname{GARCH}(1,1)$ model coefficients. As we learned, GARCH models do a great job of modelling volatility clustering, so the estimate of $\delta_{1}$ does not necessarily have to be higher than $\delta_{2}$.

The estimate of $\eta_{1}$ is suggesting a significant presence of asymmetry in the return series. It confirms that bad shocks have a much stronger effect on the stock market than positive ones. The sum of $\alpha_{1}$ and $\beta_{1}$ is about 0.96 , this number is often regarded as the persistence of the model and is generally close to 1 , implying that the volatility is persistent and is likely to be estimated very closely to the previous observation. This is mainly driven by a much higher estimate of $\beta_{1}(0.81)$, which is more tied to the persistence of volatility as it estimates based on previous observation directly. The $\alpha_{1}(0.15)$ estimate tells us more about the impact of new information in the form of disturbance $a_{t}$, and in our case, it also includes the information about asymmetry.

### 5.3 Sectoral T-GARCH results

In this section, we applied the same procedure as in Section 5.2 to all eleven sectors of the S\&P 500 index, and we will evaluate the results of both the included mean $\operatorname{AR}(\mathrm{p})$ model and the volatility T-GARCH $(1,1)$ model itself. In Appendix, the reader can find ACF for the sectors' return series.

### 5.3.1 Mean model results

Table 5.4 shows the results for the included $\mathrm{AR}(\mathrm{p})$ mean model in the TGARCH model. The order of p was chosen by minimising the information criteria for each of the sector. The majority of the sectors have four or even five autoregressive coefficients included in the model. However, for the IT, CMS and ENRG sectors, we only have a simple $\operatorname{AR}(1)$ model. In the case of IT and CMS sectors, we see slightly negative significant estimates similarly as for the whole S\&P 500. Energy sector shows an insignificant estimate of 0.008 for $\phi_{1}$. This does not provide any information and shows that the sector is tough to predict. Similarly, HC, IND, CD and MAT sectors do not have any significant estimates of the autoregressive coefficients.
Table 5.4: T-GARCH mean model results

|  | $\phi_{0}$ | $\phi_{1}$ | $\phi_{2}$ | $\phi_{3}$ | $\phi_{4}$ | $\phi_{5}$ | $\gamma_{1}$ | $\gamma_{2}$ | $\gamma_{3}$ | $\gamma_{4}$ | $\gamma_{5}$ | $\gamma_{6}$ | $\gamma_{7}$ | 8 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| SP500 | $\begin{gathered} 7.4 \mathrm{E}-4^{* *} \\ (3.5 \mathrm{E}-4) \end{gathered}$ | $\begin{array}{r} -0.071^{* *} \\ (0.034) \end{array}$ | $\begin{array}{r} 0.024 \\ (0.034) \end{array}$ | $\begin{array}{r} 0.018 \\ (0.040) \end{array}$ | $\begin{gathered} -0.009 \\ (0.034) \end{gathered}$ | - | $\begin{array}{r} \hline-0.0068 \\ (0.0053) \end{array}$ | $\begin{array}{r} 0.0031^{* * *} \\ (0.0009) \end{array}$ | $\begin{gathered} -0.0041 \\ (0.0050) \end{gathered}$ | $\begin{gathered} -0.0004 \\ (0.0019) \end{gathered}$ | $\begin{array}{r} -0.0007 \\ (0.0005) \end{array}$ | $\begin{array}{r} 0.0004 \\ (0.0007) \end{array}$ | $\begin{array}{r} 0.0020^{* * *} \\ (0.0007) \end{array}$ | $\begin{array}{r} -0.0006 \\ (0.0006) \end{array}$ |
| IT | $\begin{array}{r} 1.3 \mathrm{E}-3^{* * *} \\ (4.3 \mathrm{E}-4) \end{array}$ | $\begin{array}{r} -0.108^{* * *} \\ (0.037) \end{array}$ | - | - | - | - | $\begin{array}{r} -0.0043 \\ (0.0101) \end{array}$ | $\begin{array}{r} 0.0059^{* * *} \\ (0.0012) \end{array}$ | $\begin{gathered} \hline-0.0089 \\ (0.0103) \end{gathered}$ | $\begin{gathered} -0.0004 \\ (0.0027) \end{gathered}$ | $\begin{gathered} \hline-0.0010 \\ (0.0007) \end{gathered}$ | $\begin{array}{r} 0.0001 \\ (0.0011) \end{array}$ | $\begin{array}{r} 0.0022 \\ (0.0050) \end{array}$ | $\begin{array}{r} -0.0022^{* * *} \\ (0.0008) \end{array}$ |
| HC | $\begin{array}{r} 4.1 \mathrm{E}-4 \\ (3.7 \mathrm{E}-4) \end{array}$ | $\begin{array}{r} -0.007 \\ (0.027) \end{array}$ | $\begin{array}{r} 0.047 \\ (0.037) \end{array}$ | $\begin{gathered} \hline-0.016 \\ (0.032) \end{gathered}$ | $\begin{gathered} -0.038 \\ (0.026) \end{gathered}$ | - | $\begin{array}{r} -0.0049 \\ (0.0084) \end{array}$ | $\begin{array}{r} \hline 0.0023^{* * *} \\ (0.0008) \end{array}$ | $\begin{gathered} -0.0015 \\ (0.0086) \end{gathered}$ | $\begin{gathered} -0.0002 \\ (0.0018) \end{gathered}$ | $\begin{array}{r} \hline-0.0012^{* *} \\ (0.0005) \end{array}$ | $\begin{array}{r} \hline 0.0012 \\ (0.0007) \end{array}$ | $\begin{array}{r} \hline 0.0004 \\ (0.0038) \end{array}$ | $\begin{gathered} -0.0004 \\ (0.0007) \end{gathered}$ |
| CD | $\begin{array}{r} 9.0 \mathrm{E}-4 \\ (8.0 \mathrm{E}-4) \end{array}$ | $\begin{gathered} -0.042 \\ (0.035) \end{gathered}$ | $\begin{array}{r} 0.001 \\ (0.034) \end{array}$ | - | - | - | $\begin{array}{r} -0.0026 \\ (0.0065) \end{array}$ | $\begin{array}{r} 0.0040 \\ (0.0025) \end{array}$ | $\begin{array}{r} \hline-0.0064^{* * *} \\ (0.0015) \end{array}$ | $\begin{array}{r} -0.0020 \\ (0.0018) \end{array}$ | $\begin{array}{r} \hline-0.0006 \\ (0.0011) \end{array}$ | $\begin{array}{r} -0.0001 \\ (0.0013) \end{array}$ | $\begin{gathered} 0.0025^{* *} \\ (0.0012) \end{gathered}$ | $\begin{array}{r} -0.0001 \\ (0.0013) \end{array}$ |
| IND | $\begin{gathered} -3.2 \mathrm{E}-4 \\ (3.5 \mathrm{E}-4) \end{gathered}$ | $\begin{array}{r} 0.022 \\ (0.036) \end{array}$ | $\begin{array}{r} 0.007 \\ (0.035) \end{array}$ | $\begin{gathered} -0.006 \\ (0.037) \end{gathered}$ | $\begin{gathered} -0.023 \\ (0.036) \end{gathered}$ | - | $\begin{gathered} -0.0086 \\ (0.0090) \end{gathered}$ | $\begin{array}{r} 0.0018 \\ (0.0026) \end{array}$ | $\begin{gathered} -0.0036 \\ (0.0098) \end{gathered}$ | $\begin{array}{r} 0.0023 \\ (0.0024) \end{array}$ | $\begin{gathered} \hline-0.0002 \\ (0.0010) \end{gathered}$ | $\begin{gathered} 0.0019^{* *} \\ (0.0008) \end{gathered}$ | $\begin{array}{r} 0.0015 \\ (0.0052) \end{array}$ | $\begin{array}{r} 0.0002 \\ (0.0011) \end{array}$ |
| CS | $\begin{array}{r} 1.8 \mathrm{E}-4 \\ (3.7 \mathrm{E}-4) \end{array}$ | $\begin{array}{r} \hline-0.079^{* *} \\ (0.038) \end{array}$ | $\begin{gathered} -0.011 \\ (0.037) \end{gathered}$ | $\begin{array}{r} 0.023 \\ (0.036) \end{array}$ | $\begin{gathered} \hline-0.066^{*} \\ (0.037) \end{gathered}$ | - | $\begin{gathered} \hline-0.0022 \\ (0.0060) \end{gathered}$ | $\begin{array}{r} 0.0020 \\ (0.0016) \end{array}$ | $\begin{array}{r} 0.0005 \\ (0.0017) \end{array}$ | $\begin{array}{r} \hline-0.0001 \\ (0.0017) \end{array}$ | $\begin{gathered} \hline-0.0009 \\ (0.0008) \end{gathered}$ | $\begin{array}{r} 0.0012 \\ (0.0008) \end{array}$ | $\begin{array}{r} 0.0003 \\ (0.0014) \end{array}$ | $\begin{gathered} \hline-0.0002 \\ (0.0007) \end{gathered}$ |
| FIN | $\begin{array}{r} -7.0 \mathrm{E}-4 \\ (4.4 \mathrm{E}-4) \end{array}$ | $\begin{gathered} 0.004 \\ (0.032) \end{gathered}$ | $\begin{gathered} 0.073^{* *} \\ (0.029) \end{gathered}$ | $\begin{array}{r} 0.014 \\ (0.034) \end{array}$ | $\begin{gathered} -0.010 \\ (0.032) \end{gathered}$ | - | $\begin{array}{r} -0.0096 \\ (0.0070) \end{array}$ | $\begin{array}{r} 0.0005 \\ (0.0027) \end{array}$ | $\begin{gathered} -0.0035 \\ (0.0060) \end{gathered}$ | $\begin{array}{r} -0.0013 \\ (0.0026) \end{array}$ | $\begin{array}{r} 0.0009 \\ (0.0009) \end{array}$ | $\begin{gathered} 0.0017^{* * *} \\ (0.0006) \end{gathered}$ | $\begin{array}{r} 0.0006 \\ (0.0011) \end{array}$ | $\begin{array}{r} 0.0009 \\ (0.0014) \end{array}$ |
| MAT | $\begin{array}{r} -6.5 \mathrm{E}-5 \\ (5.2 \mathrm{E}-4) \end{array}$ | $\begin{gathered} \hline-0.009 \\ (0.037) \end{gathered}$ | $\begin{array}{r} 0.028 \\ (0.038) \end{array}$ | $\begin{array}{r} 0.001 \\ (0.037) \end{array}$ | $\begin{gathered} -0.040 \\ (0.037) \end{gathered}$ | - | $\begin{gathered} \hline-0.0019 \\ (0.0103) \end{gathered}$ | $\begin{array}{r} \hline 0.0038 \\ (0.0028) \end{array}$ | $\begin{gathered} \hline-0.0079 \\ (0.0113) \end{gathered}$ | $\begin{array}{r} 0.0020 \\ (0.0034) \end{array}$ | $\begin{array}{r} -0.0011 \\ (0.0010) \end{array}$ | $\begin{array}{r} 0.0005 \\ (0.0012) \end{array}$ | $\begin{array}{r} 0.0007 \\ (0.0056) \end{array}$ | $\begin{array}{r} \hline 0.0003 \\ (0.0015) \end{array}$ |
| ENRG | $\begin{gathered} \hline-1.1 \mathrm{E}-3^{*} \\ (6.0 \mathrm{E}-4) \end{gathered}$ | $\begin{gathered} -0.008 \\ (0.037) \end{gathered}$ | - | - | - | - | $\begin{array}{r} \hline-0.0300^{* *} \\ (0.0152) \end{array}$ | $\begin{array}{r} \hline 0.0037 \\ (0.0048) \end{array}$ | $\begin{gathered} \hline-0.0058 \\ (0.0171) \end{gathered}$ | $\begin{array}{r} 0.0005 \\ (0.0048) \end{array}$ | $\begin{array}{r} 0.0027^{* * *} \\ (0.0010) \end{array}$ | $\begin{array}{r} 0.0004 \\ (0.0013) \end{array}$ | $\begin{array}{r} 0.0000 \\ (0.0084) \end{array}$ | $\begin{array}{r} \hline 0.0011 \\ (0.0024) \end{array}$ |
| UTIL | $\begin{gathered} 1.0 \mathrm{E}-3^{* *} \\ (4.4 \mathrm{E}-4) \end{gathered}$ | $\begin{gathered} -0.013 \\ (0.036) \end{gathered}$ | $\begin{array}{r} -0.101^{* * *} \\ (0.036) \end{array}$ | $\begin{array}{r} 0.015 \\ (0.036) \end{array}$ | $\begin{gathered} -0.065^{*} \\ (0.036) \end{gathered}$ | $\begin{gathered} 0.084^{* *} \\ (0.036) \end{gathered}$ | $\begin{array}{r} 0.0079 \\ (0.0089) \end{array}$ | $\begin{gathered} 0.0049^{*} \\ (0.0026) \end{gathered}$ | $\begin{array}{r} 0.0010 \\ (0.0121) \end{array}$ | $\begin{array}{r} 0.0007 \\ (0.0025) \end{array}$ | $\begin{array}{r} -0.0030^{* * *} \\ (0.0010) \end{array}$ | $\begin{array}{r} 0.0003 \\ (0.0009) \end{array}$ | $\begin{array}{r} -0.0045 \\ (0.0049) \end{array}$ | $\begin{gathered} -0.0014 \\ (0.0011) \end{gathered}$ |
| RE | $\begin{array}{r} 6.7 \mathrm{E}-4 \\ (4.5 \mathrm{E}-4) \end{array}$ | $\begin{gathered} -0.035 \\ (0.037) \end{gathered}$ | $\begin{array}{r} 0.001 \\ (0.037) \end{array}$ | $\begin{array}{r} 0.016 \\ (0.036) \end{array}$ | $\begin{array}{r} \hline-0.080^{* *} \\ (0.036) \end{array}$ | $\begin{array}{r} 0.035 \\ (0.037) \end{array}$ | $\begin{array}{r} \hline 0.0000 \\ (0.0092) \end{array}$ | $\begin{array}{r} \hline 0.0030 \\ (0.0024) \end{array}$ | $\begin{array}{r} \hline 0.0009 \\ (0.0108) \end{array}$ | $\begin{array}{r} \hline 0.0023 \\ (0.0024) \end{array}$ | $\begin{gathered} \hline-0.0018^{*} \\ (0.0010) \end{gathered}$ | $\begin{gathered} \hline-0.0002 \\ (0.0009) \end{gathered}$ | $\begin{array}{r} 0.0006 \\ (0.0048) \end{array}$ | $\begin{gathered} \hline-0.0009 \\ (0.0011) \end{gathered}$ |
| CMS | $\begin{array}{r} 8.3 \mathrm{E}-5 \\ (4.3 \mathrm{E}-4) \\ \hline \end{array}$ | $\begin{array}{r} -0.092^{* *} \\ (0.036) \\ \hline \end{array}$ | - | - | - | - | $\begin{array}{r} \hline-0.0023 \\ (0.0092) \\ \hline \end{array}$ | $\begin{array}{r} 0.0017 \\ (0.0024) \end{array}$ | $\begin{array}{r} 0.0002 \\ (0.0056) \end{array}$ | $\begin{gathered} -0.0016^{*} \\ (0.0010) \end{gathered}$ | $\begin{array}{r} -0.0005 \\ (0.0011) \end{array}$ | $\begin{array}{r} 0.0008 \\ (0.0008) \end{array}$ | $\begin{array}{r} 0.0000 \\ (0.0044) \\ \hline \end{array}$ | $\begin{array}{r} 0.0008 \\ (0.0007) \end{array}$ |

[^3]The intercepts show us a significant positive linear trend for the IT and UTIL sectors, suggesting that they have enjoyed a growing trend since 2018. IT sector has been a hot topic dominating the US stock market in the past year, so this result comes as no suprise. The Energy sector, on the other hand, has a significantly negative intercept.

The included dummy variables show very few significant results, which are very similar across sectors. For the Monday effect during the stock market crash, we see a strong negative relationship for most sectors. However, the estimate is significant only for the Energy sector, which shows an estimate of -0.03. The Friday effect during the pandemic also shows negative insignificant results for the majority of sectors, but the relationship is much weaker. The one sector where we see something completely different is the Consumer Discretionary sector, which has a significant estimate of -0.0064 for the Friday effect during the pandemic, as opposed to a insignificant estimate of -0.0026 for Mondays. It implies that the inflow of bad news during weekends might not have affected the CD sector as much as the other sectors.

The overall Monday and Friday effects for the whole timeline show supporting evidence to the existing literature as the Monday effect is mostly negative. In contrast, the Friday effect is slightly positive. Even though most of the estimates are insignificant, we can definitely still observe some inefficiency on the market, especially for the IND and FIN sectors, which have significant estimates of 0.0019 and 0.0017 , respectively, for the Friday effect.

The Information Technology sector shows very high and significant Monday returns for the period after the crash. Since the whole S\&P 500 index also shows big positive Monday returns for the given period, it is not surprising as the IT sector enjoyed a very successful year in 2020 on the US stock market. Surprisingly though, no other sector has a significant (at $5 \%$ level of significance) result for Monday returns in that period, but the results are still positive for all of them.

### 5.3.2 STD model results

The results in Table 5.5 were obtained by estimating the T-GARCH $(1,1)$ model. Each sector has a specific included mean model based on the results in the previous subsection. Apart from the estimated coefficients, we can also find the Akaike information criteria in the last column, which tells us how good of a fit the model is. Equation 4.8 shows the standard calculation for AIC, however,

Table 5.5: T-GARCH volatility model results

|  | $\alpha_{0}$ | $\alpha_{1}$ | $\beta_{1}$ | $\eta_{1}$ | $\delta_{1}$ | $\delta_{2}$ | AIC |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| SP500 | $0.0006^{* * *}$ | $0.153^{* * *}$ | $0.811^{* * *}$ | $0.875^{* * *}$ | 0.0007 | $0.0006^{* * *}$ | -6.41 |
|  | $(0.000)$ | $(0.033)$ | $(0.031)$ | $(0.198)$ | $(0.0006)$ | $(0.0001)$ |  |
| IT | $0.0009^{* * *}$ | $0.113^{* * *}$ | $0.836^{* * *}$ | $0.881^{* * *}$ | $0.0015^{*}$ | $0.0008^{* * *}$ | -5.71 |
|  | $(0.000)$ | $(0.030)$ | $(0.029)$ | $(0.252)$ | $(0.0009)$ | $(0.0002)$ |  |
| HC | $0.0006^{* * *}$ | $0.093^{* * *}$ | $0.864^{* * *}$ | $1.000^{* * *}$ | $0.0013^{*}$ | 0.0002 | -6.32 |
|  | $(0.000)$ | $(0.027)$ | $(0.029)$ | $(0.279)$ | $(0.0006)$ | $(0.0001)$ |  |
| CD | $0.0005^{* * *}$ | $0.106^{* * *}$ | $0.862^{* * *}$ | $0.737^{* * *}$ | $0.0012^{* *}$ | $0.0005^{* * *}$ | -6.09 |
|  | $(0.000)$ | $(0.023)$ | $(0.024)$ | $(0.197)$ | $(0.0005)$ | $(0.0001)$ |  |
| IND | $0.0005^{* * *}$ | $0.086^{* *}$ | $0.888^{* * *}$ | $0.922^{* *}$ | $0.0011^{*}$ | 0.0002 | -5.93 |
|  | $(0.000)$ | $(0.036)$ | $(0.042)$ | $(0.372)$ | $(0.0006)$ | $(0.0001)$ |  |
| CS | $0.0005^{* * *}$ | $0.090^{* * *}$ | $0.862^{* * *}$ | $0.863^{* * *}$ | $0.0013^{* * *}$ | 0.0001 | -6.66 |
|  | $(0.000)$ | $(0.029)$ | $(0.033)$ | $(0.305)$ | $(0.0005)$ | $(0.0001)$ |  |
| FIN | $0.0007^{* * *}$ | $0.127^{* * *}$ | $0.845^{* * *}$ | $1.000^{* * *}$ | 0.0007 | $0.0004^{* *}$ | -5.86 |
|  | $(0.000)$ | $(0.027)$ | $(0.028)$ | $(0.210)$ | $(0.0006)$ | $(0.0002)$ |  |
| MAT | 0.0006 | 0.074 | $0.886^{* * *}$ | 1.000 | $0.0017^{* *}$ | 0.0003 | -5.90 |
|  | $(0.000)$ | $(0.058)$ | $(0.079)$ | $(0.705)$ | $(0.0008)$ | $(0.0002)$ |  |
| ENRG | $0.0007^{* *}$ | $0.053^{* *}$ | $0.905^{* * *}$ | $0.940^{* *}$ | $0.0029^{* * *}$ | $0.0008^{* *}$ | -5.25 |
|  | $(0.000)$ | $(0.027)$ | $(0.038)$ | $(0.410)$ | $(0.0010)$ | $(0.0004)$ |  |
| UTIL | $0.0003^{* * *}$ | $0.026^{*}$ | $0.941^{* * *}$ | 1.000 | $0.0022^{* * *}$ | $0.0001^{* *}$ | -6.31 |
|  | $(0.000)$ | $(0.013)$ | $(0.014)$ | $(0.713)$ | $(0.0005)$ | $(0.0001)$ |  |
| RE | $0.0003^{* * *}$ | $0.043^{*}$ | $0.934^{* * *}$ | 1.000 | $0.0018^{* * *}$ | 0.0001 | -6.16 |
|  | $(0.000)$ | $(0.025)$ | $(0.027)$ | $(0.633)$ | $(0.0005)$ | $(0.0001)$ |  |
| CMS | $0.0007^{* * *}$ | $0.059^{* *}$ | $0.891^{* * *}$ | $1.000^{* *}$ | $0.0012^{* *}$ | $0.0003^{* *}$ | -5.89 |
|  | $(0.000)$ | $(0.024)$ | $(0.032)$ | $(0.447)$ | $(0.0005)$ | $(0.0001)$ |  |

Notes: *, ${ }^{* *}$, ${ }^{* *}$ stand for $10 \%, 5 \%$ and $1 \%$ level of significance respectively. Standard errors of estimates are in parenthesis.
AIC is the Akaike information criterion. $\delta_{i}$ dummies stand for: $1-\mathrm{DUR}, 2$ - AFTR
in this case, the AIC is calculated based on the following formula:

$$
A I C=\frac{-2 \ln (\hat{L})}{N}+\frac{2 k}{N}
$$

Where $\hat{L}$ is the likelihood function evaluated at the maximum likelihood estimates, k is the number of estimated parameters in the model, and N is the total number of observations.

The estimated coefficients of the model are mostly significant. Even most of the included dummy variables show at least a $10 \%$ level of significance, which is an excellent sign implying that the estimated models are very well specified,
and we can rely on the results. The AIC on its own is not telling much, as it is mostly used to evaluate when comparing competing models. For example, models like standard $\operatorname{GARCH}(1,1)$ or GJR-GARCH $(1,1)$ return AIC of -6.36 and -6.39 , respectively, for the S\&P 500 index. Since we are minimising the AIC, we know the $\operatorname{T}-\operatorname{GARCH}(1,1)$ with a value of -6.41 is marginally better. The purpose of the AIC in Table 5.5 is to illustrate that there is no sector for which we would see a struggling model with two times lower AIC than a different one.

From the $\alpha_{0}$ estimates, we can see the intercept of the volatility equation. The Information Technology sector has the highest estimate of 0.0009 , showing that the expected volatility has generally been higher than for other sectors. Interestingly, sectors with lower intercept $\alpha_{0}$ have a much greater estimate of $\delta_{1}$, reflecting the volatility rise during the pandemic crash period. It shows that even sectors with moderately lower unconditional volatility have seen a dramatic increase in volatility during the pandemic. The most significant effect is seen for the Energy sector. Its volatility increased dramatically, with an intercept of 0.0007 rising an additional 0.0029 during the pandemic and 0.0008 in the period after. The very wild ride of the Energy sector on the US stock market in 2020 was driven mainly by the unstable oil industry situation ${ }^{1}$.

While we do not have a significant estimate of $\delta_{1}$ for the S\&P 500, we can see the individual sectors' impact with $10 / 11$ significant estimates. It shows that investors can significantly decrease the risk during turbulent periods on the US stock market by broadening the portfolio. The Financials sector, which did not return a significant estimate $\delta_{1}$ is the third largest sector in terms of the number of constituents. On the other hand, sectors like ENRG, MAT, UTIL or CMS, all with less than 30 constituents, have very high and significant increases in volatility.

The estimates of $\delta_{1}$ generally show that all sectors were affected in terms of volatility during the crash period. However, the estimates of $\delta_{2}$ tell us a completely different story as some sectors continued to have increased volatility and some did not. The IND, CS, UTIL, RE, MAT, and HC sectors show very little increase in volatility in the period after the crash, it strikes as especially interesting for the Health Care sector as the pandemic is continuing throughout the whole period, and the industry was a big talking point as investors were looking to invest in healthcare companies, which will help bring the world out of

[^4]the pandemic. On the other hand, IT, FIN, CD, CMS and ENRG sectors have seen a substantial increase in volatility even after the crash period. If we look at what are the individual sectors composed of, this significant rise in volatility makes sense. IT companies have seen an extreme increase in demand due to home-office or home-schooling contrasted by the shortage of semiconductors, which understandably supports the increased volatility on the market. Banks in the financial sector are providing more unsecured loans to support affected businesses. Hotels and restaurants in the CD sector were strongly restricted in the past year. People spend more time on Netflix, YouTube and other platforms, which reflect results in the CMS sector. These are all factors why we see persistent volatility increase among those sectors.

The coefficients $\alpha_{1}$ and $\beta_{1}$ are very similar across sectors, showing that excess volatility modelling does not differ much across sectors after we account for intercepts. We see that IT and FIN sectors have higher estimates of $\alpha_{1}$ at 0.11 and 0.13 , respectively, showing that those sectors are more driven by past shocks than other sectors. On the other hand, MAT, UTIL and RE sectors have very low and even insignificant (at $5 \%$ level of significance) estimates of $\alpha_{1}$ showing that these sectors are mainly driven by previous observations of volatility, included in the $\beta_{1}$ estimate, and not driven by past shocks. Consequently, the estimates of $\eta_{1}$ for these sectors are also insignificant as they are closely tied to $\alpha_{1}$. In contrast, other sectors show high significant asymmetry with $\eta_{1}$ close to one, concluding that the market tends to react more strongly to negative shocks.

### 5.4 Intraday volume patterns

From Figure 5.5, we can see the volume traded in absolute terms on the left and daily proportions on the right. In both cases, the numbers are calculated as means for the given time period. The events triggered by the COVID19 pandemic certainly attracted a lot of investors' attention, which caused the volume of trades to increase dramatically and stay high even after the situation on the US stock market calmed down a bit after the crash.

In this part of the analysis, we are interested in the changes to daily volume proportions patterns in 30 -minute intervals. These changes are apparent from the right plot of Figure 5.5. However, we provide further analysis to test which intervals' differences are significant by employing the ANOVA method.

The change of daily pattern might be valuable information for models which

Figure 5.5: Volume traded of the USA500 index

implement volume values to forecast returns. It allows such models to change accordingly in times of unexpected events affecting the stock market.

### 5.4.1 ANOVA results

Table 5.6 shows the mean values for daily volume proportions calculated based on Equation 4.9. The values are grouped by days of the week and by time period. Values below the double-line titled "Average" are only grouped by time period. The ANOVA is employed on all groups in all 30-minute intervals.

We are interested if there is any difference between the means of the three time periods (as outlined in Section 3.2), so the null hypothesis we are trying to reject is $H_{0}: \mu_{\text {before }}=\mu_{\text {during }}=\mu_{\text {after }}$. It is important to note that we cannot conclude that one period differs significantly from another one by rejecting the null hypothesis. Instead, we conclude that the three periods together differ significantly.

Looking at the results for an average day, we can see the proportions changed significantly at all 30-minute intervals, except between $11 \mathrm{am}-12 \mathrm{pm}$,
with at least a 0.05 level of significance. The most notable change is seen in the first half hour of trading between 9:30-10 am, where we observe up to $20 \%$ of daily volume being fulfilled on Mondays and $17 \%$ on an average day in the period before the pandemic, dropping to $13 \%$ and $14 \%$ respectively in the period during the pandemic crash. The volume in the first half hour remained lower in the period after the crash as well with $14 \%$, on the other hand, this period has the highest volume of trades being fulfilled in the last 30 minutes of trading at $10 \%$ of the total daily volume.

Overall, we see the patterns changed significantly, mainly for a trading day's early and late hours. The most significant changes are on Mondays, which is understandable for the early hours as the market responds to news happening during weekends. However, interestingly the changes are also very significant throughout the whole day. On the other hand, we see only one significant change on Wednesday.

From the results, we can confidently conclude that the daily volume Ushaped curve flattened during the pandemic, as the stock market's attention was spread out more evenly. It would be interesting to obtain volume data for specific types of investors to see better what causes this change in pattern. It might very well be caused by individual investors, who perhaps do not pay much attention to their trades' timings. Whereas institutional investors often realise the trades in the first and last minutes of trading.
Table 5.6: Results of the ANOVA for 30-minute interval average proportions of daily volume

| $9: 30-10: 00$ | $10: 00-10: 30$ | $10: 30-11: 00$ | $11: 00-11: 30$ | $11: 30-12: 00$ | $12: 00-12: 30$ | $12: 30-13: 00$ | $13: 00-13: 30$ | $13: 30-14: 00$ | $14: 00-14: 30$ | $14: 30-15: 00$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $15: 00-15: 30$ | $15: 30-16: 00$ |  |  |  |  |  |  |  |  |  |


| Monday | Before | 0.20 (0.05) | 0.13 (0.03) | 0.10 (0.02) | 0.09 (0.02) | 0.07 (0.02) | 0.06 (0.01) | 0.05 (0.01) | 0.04 (0.01) | 0.04 (0.02) | 0.04 (0.02) | 0.04 (0.02) | 0.05 (0.02) | 0.09 (0.03) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | During | 0.13 (0.07) | 0.15 (0.1) | 0.08 (0.03) | 0.08 (0.03) | 0.08 (0.03) | 0.08 (0.02) | 0.06 (0.02) | 0.06 (0.02) | 0.05 (0.02) | 0.06 (0.02) | 0.05 (0.03) | 0.05 (0.02) | 0.07 (0.01) |
|  | After | 0.15 (0.05) | 0.11 (0.03) | 0.09 (0.02) | 0.08 (0.02) | 0.07 (0.02) | 0.06 (0.02) | 0.05 (0.01) | 0.05 (0.01) | 0.05 (0.01) | 0.06 (0.02) | 0.06 (0.02) | 0.07 (0.02) | 0.10 (0.03) |
|  | F-Test | 13.9*** | 4.9*** | 3.3** | 3.6** | 0.8 | 5.4*** | $3.7{ }^{* *}$ | $7.8^{* * *}$ | 2.8* | $8.6{ }^{* * *}$ | 9.6*** | 18.6*** | $5^{* * *}$ |
| Tuesday | Before | 0.17 (0.06) | 0.12 (0.03) | 0.10 (0.03) | 0.08 (0.03) | 0.07 (0.02) | 0.06 (0.02) | 0.05 (0.02) | 0.05 (0.02) | 0.05 (0.03) | 0.05 (0.02) | 0.05 (0.03) | 0.06 (0.02) | 0.09 (0.03) |
|  | During | 0.14 (0.09) | 0.11 (0.08) | 0.09 (0.05) | 0.10 (0.05) | 0.07 (0.03) | 0.07 (0.03) | 0.05 (0.03) | 0.05 (0.04) | 0.05 (0.03) | 0.06 (0.03) | 0.06 (0.03) | 0.07 (0.03) | 0.09 (0.04) |
|  | After | 0.14 (0.03) | 0.11 (0.02) | 0.09 (0.02) | 0.09 (0.02) | 0.07 (0.02) | 0.06 (0.02) | 0.05 (0.01) | 0.05 (0.01) | 0.05 (0.01) | 0.05 (0.01) | 0.06 (0.02) | 0.08 (0.03) | 0.11 (0.03) |
|  | F-Test | 6.3*** | 2.6* | 0.5 | 0.6 | 0.5 | 0.4 | 0.2 | 0.5 | 0 | 1.4 | 2.2 | 9.2*** | 4.2** |
| Wednesday | Before | 0.16 (0.05) | 0.12 (0.05) | 0.09 (0.03) | 0.08 (0.03) | 0.07 (0.03) | 0.05 (0.02) | 0.05 (0.02) | 0.04 (0.02) | 0.04 (0.02) | 0.08 (0.06) | 0.07 (0.06) | 0.07 (0.04) | 0.09 (0.03) |
|  | During | 0.13 (0.07) | 0.10 (0.05) | 0.09 (0.05) | 0.07 (0.03) | 0.06 (0.02) | 0.07 (0.03) | 0.05 (0.01) | 0.05 (0.02) | 0.07 (0.04) | 0.07 (0.03) | 0.07 (0.04) | 0.07 (0.03) | 0.10 (0.02) |
|  | After | (0.04) | .03) | .03) | (02) | 2) | .02) | (02) | (02) | (0.02) | (0.03) | 0.07 (0.03) | (0.03) | 0.03) |
|  | F-Test | 2.4* | 0.8 | 0.4 | 0.2 | 1 | 0.8 | 0.5 | 1.7 | 5.3*** | 0.1 | 0.1 | 1.6 | 2 |
| Thursday | for | 0.17 (0.05) | 0.12 (0.04) | 0.10 (0.03) | 0.09 (0.03) | 0.07 (0.02) | 0.06 (0.02) | 0.05 (0.02) | 0.04 (0.02) | 0.05 (0.03) | 0.05 (0.02) | (0.04) | 0. 06 (0.03) | (0.03) |
|  | During | 0.10 (0.06) | 0.10 (0.06) | 0.08 (0.04) | 0.07 (0.03) | 0.10 (0.07) | 0.08 (0.04) | 0.08 (0.03) | 0.08 (0.03) | . 77 (0.04) | 0.06 (0.04) | 0.06 (0.03) | 0.06 (0.02) | 0.06 (0.02) |
|  | After | 0.13 (0.04) | 0.10 (0.03) | 0.09 (0.02) | 0.08 (0.02) | 0.07 (0.01) | 0.06 (0.01) | 0.06 (0.02) | 0.06 (0.02) | 0.05 (0.02) | 0.06 (0.02) | 0.06 (0.02) | 0.07 (0.02) | 0.10 (0.03) |
|  | F-Test | 13.1*** | 4.1** | 1.9 | 1.1 | 4.4** | 3.8** | 5.8*** | 13.3*** | 2.7 * | 3.6** | . 4 | 6.9** | 4.9*** |
| Friday | Before | 0.17 (0.05) | 0.13 (0.04) | 0.10 (0.03) | 0.09 (0.02) | 0.08 (0.03) | 0.06 (0.02) | 0.05 (0.02) | 0.05 (0.03) | 0.04 (0.02) | 0.05 (0.02) | 0.04 (0.02) | 0.05 (0.02) | 0.10 (0.03) |
|  | During | 0.17 (0.07) | 0.12 (0.04) | 0.10 (0.04) | 0.08 (0.03) | 0.06 (0.02) | 0.05 (0.02) | 0.05 (0.02) | 0.05 (0.02) | 0.05 (0.02) | 0.06 (0.02) | 0.06 (0.02) | 0.06 (0.02) | 0.09 (0.02) |
|  | After | 0.14 (0.04) | 0.11 (0.03) | 0.09 (0.02) | 0.08 (0.02) | 0.07 (0.02) | 0.06 (0.02) | 0.06 (0.02) | 0.05 (0.02) | 0.05 (0.02) | 0.06 (0.02) | 0.06 (0.02) | 0.07 (0.02) | 0.09 (0.02) |
|  | F-Test | 3.9** | 4.7** | 0.1 | 0.9 | 2.8* | 1.4 | 1.6 | 0.5 | 2.4* | 4.8*** | 9.2*** | $9^{* *}$ | 0.3 |
| Average | Before | 0.17 (0.06) | 0.12 (0.04) | 0.10 (0.03) | 0.08 (0.03) | 0.07 (0.02) | 0.06 (0.02) | 0.05 (0.02) | 0.04 (0.02) | 0.04 (0.02) | 0.05 (0.04) | 0.05 (0.04) | 0.06 (0.03) | 0.09 (0.03) |
|  | During | 0.14 (0.08) | 0.11 (0.07) | 0.09 (0.04) | 0.08 (0.03) | 0.07 (0.04) | 0.07 (0.03) | 0.06 (0.03) | 0.06 (0.03) | 0.06 (0.03) | 0.06 (0.03) | 0.06 (0.03) | 0.06 (0.03) | 0.08 (0.03) |
|  | After | 0.14 (0.04) | 0.11 (0.03) | 0.09 (0.02) | 0.08 (0.02) | 0.07 (0.02) | 0.06 (0.02) | 0.05 (0.02) | 0.05 (0.02) | 0.05 (0.02) | 0.06 (0.02) | 0.06 (0.02) | 0.08 (0.03) | 0.10 (0.03) |
|  | Test | $31.3^{* * *}$ | 12.6*** | 3.9** | 2.4* | 2.2 | $3.3^{* *}$ | 6.3 *** | 11.4*** | $9.2{ }^{* * *}$ | $4.8{ }^{* * *}$ | 6.9 *** | $31.2{ }^{* * *}$ | $11^{* *}$ |

Notes: F-Test value corresponds to the outcome of ANOVA testing method mentioned in the methodology. Standard deviation is in parenthesis
$*, * * * * *$ stand for
*, ${ }^{* *},{ }^{* * *}$ stand for $10 \%, 5 \%$ and $1 \%$ level of significance respectively, at which we reject the $H_{0}: \mu_{1}=\mu_{2}=\mu_{3}$

## Chapter 6

## Conclusion

This work brings interesting results of pattern changes on the US stock market as a response to the COVID-19 pandemic, which has caused the market to crash heavily in March 2020. While the pandemic has been evolving every second, the US stock market is open for trading only during certain hours a day and is closed on weekends. This discrepancy of no trading during weekends, while there is a ton of new information being released, is the primary motivation why we focus mainly on the Monday and Friday effect. We employ the T-GARCH $(1,1)$ model on a return series of the S\&P 500 index and its eleven sectors. Our dataset runs from the beginning of 2018 until March 15, 2021, and by using dummy variables, we divide the timeline into three periods. The main period during the pandemic crash runs from February 3, 2020, just after the Trump administration declared a national public health emergency, to March 20, 2020, as the last observation before the FED announced unlimited quantitative easing.

Our results show significantly higher values of volatility during the crash across all sectors. Interestingly, some sectors show very little increase in volatility for the period after the crash, while heavily affected sectors by the pandemic like the Information technology, Financials, Consumer discretionary, Energy and Communication services, which have seen some major disruptions caused by the pandemic ${ }^{1}$, show lasting impact in volatility levels. It is an excellent representation of how the pandemic affected various types of businesses in a long-term perspective and provides a great insight for investors, who can use this knowledge to better calculate the risks associated with businesses operating in the affected areas of the economy. Unfortunately, the results regarding Mon-

[^5]day and Friday effects are mostly insignificant. However, we can still observe a pattern that the Monday returns during the crash were lower than Friday ones. On the other hand, the results are reversed for the bull market after the crash, where the estimates for Monday returns are generally higher than for Friday returns. This finding supports the calendar time hypothesis (French 1980), where the Monday returns include the returns of the two non-trading days and thus are higher than for other days of the week.

The thesis also analyses the investors' behaviour in terms of intraday volume trading patterns. Using 30 -minute data, we observed the proportions of daily trading happening in half-hour intervals of a trading day. Using statistical analysis, we can confidently conclude that the trading pattern has changed across the observed three periods. The results show that before the pandemic crash, almost one-fifth of all daily trades happened in the first half-hour of trading between 9:30-10:00 AM. However, in the periods during and after the crash, the proportions evened out by a considerable margin. The standard Ushape pattern for daily trading has flattened during the pandemic crash as more of the volume took place throughout the whole day, but the biggest proportion of trades still happened in the first half-hour of trading for all periods.

Finally, we would like to point out topics for further research based on our analysis. As the results of the day-of-the-week effect are not significant enough to make firm conclusions, it would be interesting to see if that would change with more observations for the crash period. Unfortunately, the market quickly started recovering, and there is no way to obtain more daily observations. Nevertheless, working with high-frequency data might bring some more precise results for the Monday and Friday effects. For next research, it might also be interesting to look deeper into the intraday volume analysis as having data on the investor's type might tell us more about the causes of the pattern changes. Knowing whether institutional investors or small investors drove the change might help us better understand the effects of the COVID-19 pandemic on the US stock market.

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## Appendix A

## Appendix A - tables

Table A.1: P-values of ADF and KPSS tests

|  | ADF |  | KPSS |  |
| :--- | :---: | :---: | :---: | :---: |
|  | Level | Log-return | Level | Log-return |
| SP500 | 0.34 | $<0.01$ | $<0.01$ | $>0.1$ |
| IT | 0.54 | $<0.01$ | $<0.01$ | $>0.1$ |
| HC | 0.02 | $<0.01$ | $<0.01$ | $>0.1$ |
| CD | 0.49 | $<0.01$ | $<0.01$ | $>0.1$ |
| IND | 0.49 | $<0.01$ | $<0.01$ | $>0.1$ |
| CS | $<0.01$ | $<0.01$ | $<0.01$ | $>0.1$ |
| FIN | 0.61 | $<0.01$ | 0.019 | $>0.1$ |
| MAT | 0.74 | $<0.01$ | $<0.01$ | $>0.1$ |
| ENRG | 0.46 | $<0.01$ | $<0.01$ | $>0.1$ |
| UTIL | 0.03 | $<0.01$ | $<0.01$ | $>0.1$ |
| RE | 0.06 | $<0.01$ | $<0.01$ | $>0.1$ |
| CMS | 0.54 | $<0.01$ | $<0.01$ | $>0.1$ |

Table A.2: List of excluded days in the intraday volume analysis

| Holiday / Shortened hours | 2019 | $\mathbf{2 0 2 0}$ | $\mathbf{2 0 2 1}$ |
| :--- | ---: | ---: | ---: |
| New Year's Day | January 1, 2019 | January 1, 2020 | January 1, 2021 |
| Martin Luther King, Jr. Day | January 21, 2019 | January 20, 2020 | January 18, 2021 |
| Washington's Birthday | February 18, 2019 | February 17, 2020 | February 15, 2021 |
| Good Friday | April 19, 2019 | April 10, 2020 |  |
| Memorial Day | May 27, 2019 | May 25, 2020 |  |
| shortened hours | July 3, 2019 |  |  |
| Independence Day | July 4, 2019 | July 3, 2020 |  |
| Labor Day | September 2, 2019 | September 7, 2020 |  |
| Thanksgiving Day | November 28, 2019 | November 26, 2020 |  |
| shortened hours | November 29, 2019 | November 27, 2020 |  |
| shortened hours | December 24, 2019 | December 24, 2020 |  |
| Christmas Day | December 25, 2019 | December 25, 2020 |  |

## Appendix B

## Appendix B - figures

Figure B.1: ACF and PACF of IT sector daily log returns


Figure B.2: ACF and PACF of HC sector daily log returns



Figure B.3: ACF and PACF of CD sector daily log returns


Figure B.4: ACF and PACF of IND sector daily log returns


Figure B.5: ACF and PACF of CS sector daily log returns



Figure B.6: ACF and PACF of FIN sector daily log returns


Figure B.7: ACF and PACF of MAT sector daily log returns


Figure B.8: ACF and PACF of ENRG sector daily log returns


Figure B.9: ACF and PACF of UTIL sector daily log returns


Figure B.10: ACF and PACF of RE sector daily $\log$ returns


Figure B.11: ACF and PACF of CMS sector daily log returns



[^0]:    ${ }^{1}$ Bear market describes the state of the market in which prices are declining and is often more volatile as opposed to bull market in which the prices are rising and volatility declines.
    ${ }^{2}$ Short for Federal Reserve is the central banking system in the USA.

[^1]:    ${ }^{1}$ https://www.spglobal.com/spdji/en/landing/investment-themes/sectors/
    ${ }^{2}$ https://www.dukascopy.com/swiss/cz/marketwatch/historical/
    ${ }^{3}$ shares which can be publicly traded and are not restricted, i.e. not held by company management

[^2]:    ${ }^{4}$ Pre-market trading is trading that occurs between 4 a.m. and 9:30 a.m. EST

[^3]:    Notes: ${ }^{*},{ }^{* *}, * * *$ stand for $10 \%, 5 \%$ and $1 \%$ level of significance respectively. Standard errors of estimates are in parenthes.
    $\gamma_{i}$ dummies stand for: $1-\mathrm{DUR}^{*}$ Mon, $2-\mathrm{AFTR}^{*}$ Mon, $3-\mathrm{DUR}^{*}$ Fri, $4-\mathrm{AFTR}^{*}$ Fri, $5-\mathrm{Mon}, 6-\mathrm{Fri}, 7-\mathrm{DUR}, 8-\mathrm{AFTR}$

[^4]:    ${ }^{1}$ Saudi Arabia announced unexpected oil price discounts on March 8, 2020, which caused the oil prices to plummet dramatically. On April 20, some oil prices even went below zero.

[^5]:    ${ }^{1}$ IT - shortage of semiconductors, FIN - more unsecured loans to affected businesses, CD - heavy restrictions on hotels and restaurants, ENRG - oil prices falling below zero at one point, CMS - people spending more time online

