In this thesis we study geometry of Poisson-Lie T-duality. We develop the language of Lie and Courant algebroids and study generalized metrics on them. Then we use Dirac structures and generalized isometries to formulate a general version of Poisson-Lie T-duality, a non-abelian version of T-duality, known from string theory.