

We study questions concerning convexity and the existence of the nearest point for a given set in spaces equipped with either a norm, or with a more general functional, namely a quasinorm or an α -norm. We characterize convexity in a Hilbert space. We investigate relations between convexity and properties of the distance function.