

This thesis concerns following hypothesis: whenever I is two-sided idempotent ideal in group ring $\mathbb{Z}S_n$, such that $I\mathbb{Q}$ is non-trivial ideal of $\mathbb{Q}S_n$, $I\mathbb{Q}$ has to be so called augmentation ideal. The validity of this hypothesis would give us weak version of the fact that in the case of solvable group G , there are no two-sided non-trivial idempotent ideals in $\mathbb{Z}G$. At first I describe method how to calculate idempotent ideals in $\mathbb{Z}S_n$ and then show that hypothesis holds in the case of S_5 , but fail in the case of $\mathbb{Z}S_5$. In theoretic part, I firstly switch to local point of view and describe two-sided idempotent ideals in $\mathbb{Z}_{(p)}S_n$, for primes p dividing order of group S_n , as trace ideals of finitely generated projective $\mathbb{Z}_{(p)}S_n$ -modules. Next, I describe functor $-\otimes_{\mathbb{Z}_{(p)}}\mathbb{Q} : Proj(\mathbb{Z}_{(p)}S_n) \rightarrow Mod(\mathbb{Q}S_n)$ using the language of Grothendieck groups by matrix E . Matrix E shows to be transposition of decomposition matrix, which we can calculate using Brauer's character.