We study algebraic tools for proving the existence of graph colorings and focus a classical method of Alon-Tarsi from this area. In particular, we prove Alon-Tarsi Theorem, provide examples of some known applications and give a new application to colorings of squares of cycles.