In this thesis, we look for sufficient conditions for non-absolute convergence of Newton integral. Importantly we analyse how the oscillation of the sine function influences the convergence of the integral. We are dealing with the convergence of integrals based on the limits of the antiderivative, which does not need to convergence in the Lebesgue sense.